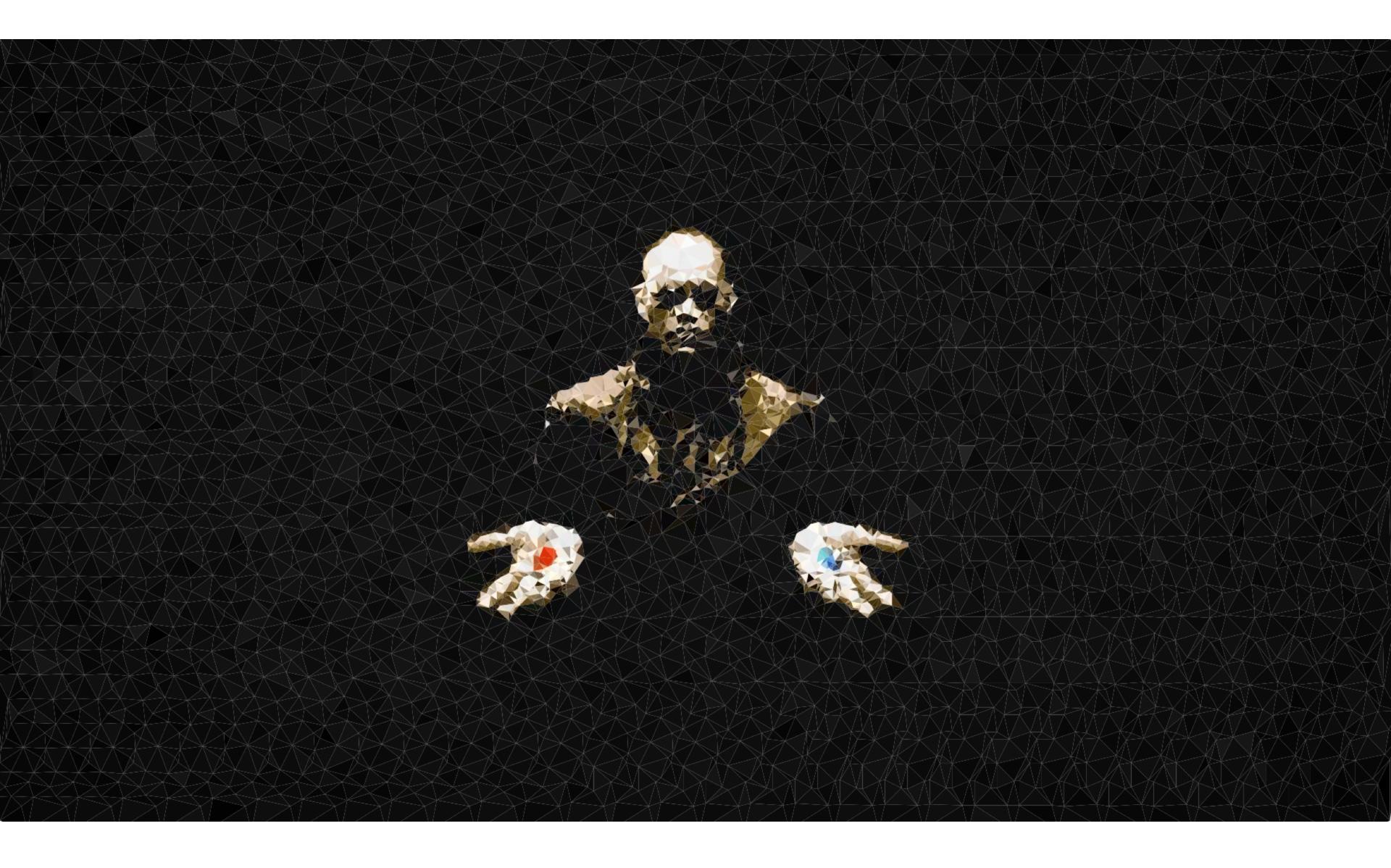
Lecture 11

Introduction to Animation

Interactive Computer Graphics Stanford CS248, Winter 2020

Cool SVGs



by Mustafa Bayramov

Cool SVGs



by Oliva Hsu and Taeyoung Kong



Exam information

- There is no final exam during the final exam slot
- There is a "single exam" which <u>was</u> scheduled for the evening of March 3rd (to allow for a full two-hour exam)
 - However, this turns out to be primary election night
 - So we need to move it
 - I would like to move it to the evening of March 2nd
 - We will finalize this date in the next 48 hours
- The exam is open notes, open slides and will consist of questions like what you have seen on the practice exercises.

Final projects

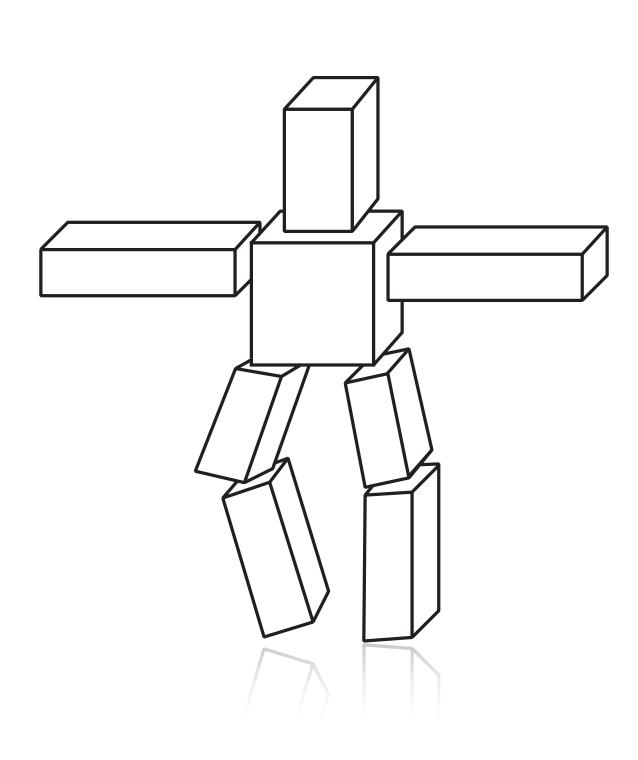
- Assignment 3 is due on 2/20
- Initial 1-2 page project proposals are due on 2/27
- Final project writeup are due on 3/18
- Final project videos are due on 3/19
 - You may do whatever you want for a final project
 - But it must be approved by the staff via the proposal
 - And we expect it to be about three weeks of solid work
 - Top grades reserved for truly great projects

Ideas

- Extend the SVG renderer from Assignment 1 so it can render as many SVG files from the web as possible. This would involve adding support for new primitive types: spline curves, ellipses, rotated images, fonts, text. Etc. We recommend that you start by downloading some interesting SVG's and then continue to add features to your SVG renderer until it correctly renders them.
- Implement all of the extra credits for Assignment 2 (if you haven't done so already) such as mesh beveling, mesh decimation, etc. and use the resulting modeling tool to create a really cool mesh. A good way to design the project is to first pick a mesh you want to create, and then add features to your tool to make it.
- Complete the Animation part of Assignment 2. (It is described on the Assignment 2 wiki.) This involves inverse kinematics, mass-spring systems, and keyframe animation.
- Extend Assignment 3 to render more advanced shadows and materials. For example, you could take a look at techniques like cascaded shadow maps, screen-space ambient obscurance, environment mapping (by generating a cube map), or other, more advanced types of light sources, like linear-transformed cosines or spherical harmonic lighting. Then design the coolest scene you can that shows off all the new features.
- You could write a ray tracer from scratch. Better yet, write a GPU-accelerated ray tracer from scratching using the new RTX accelerated APIs

Project videos!

Increasing the complexity of our model of the world Materials, lighting, ... **Transformations** Geometry





Increasing the complexity of our model of the world ...but what about *motion*?



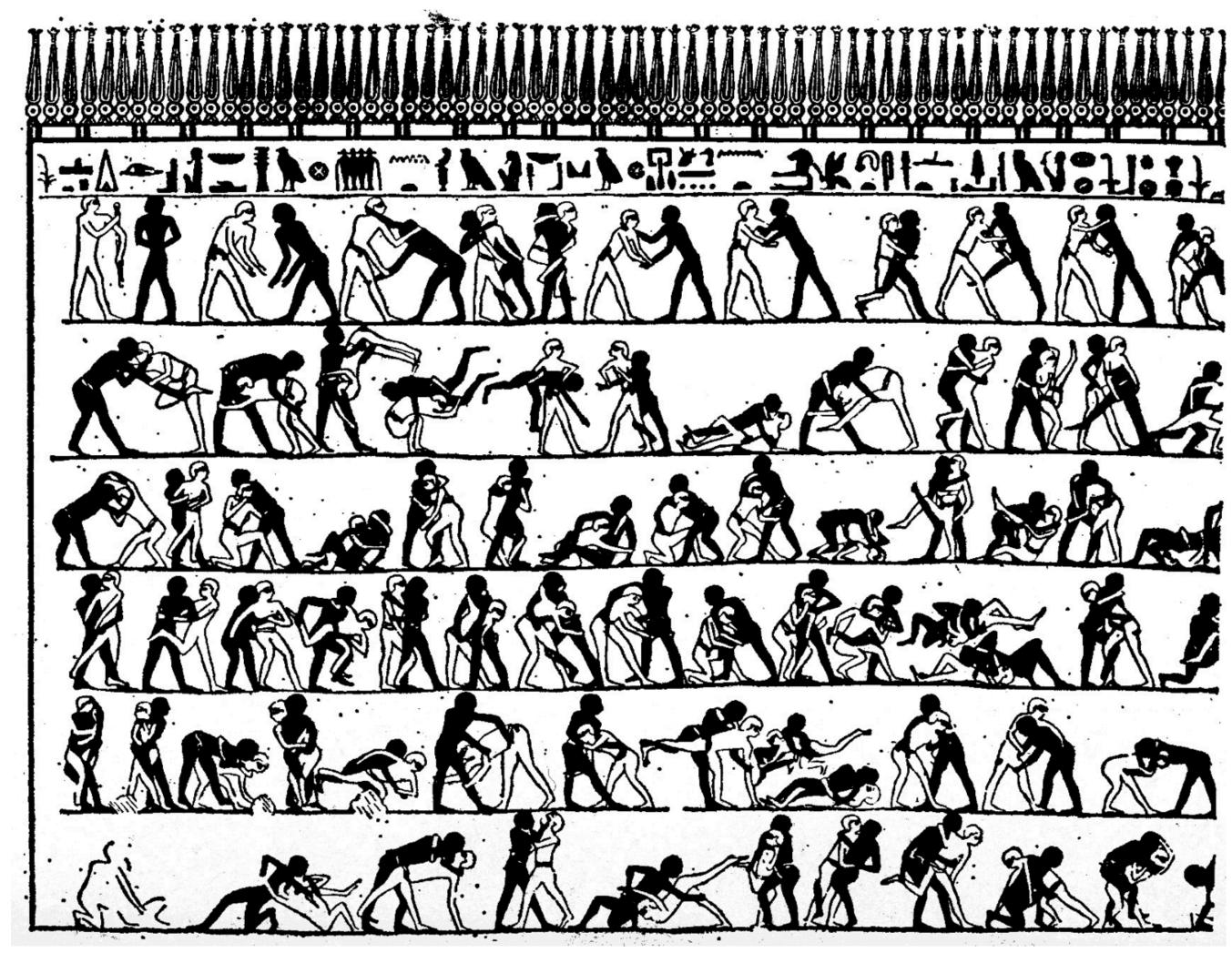
First animation





(Shahr-e Sukhteh, Iran 3200 BCE)

History of animation



(tomb of Khnumhotep, Egypt 2400 BCE)

History of animation



(Phenakistoscope, 1831)

First film

Originally used as scientific tool rather than for entertainment Critical technology that accelerated development of animation



Eadweard Muybridge, "Sallie Gardner" (1878)

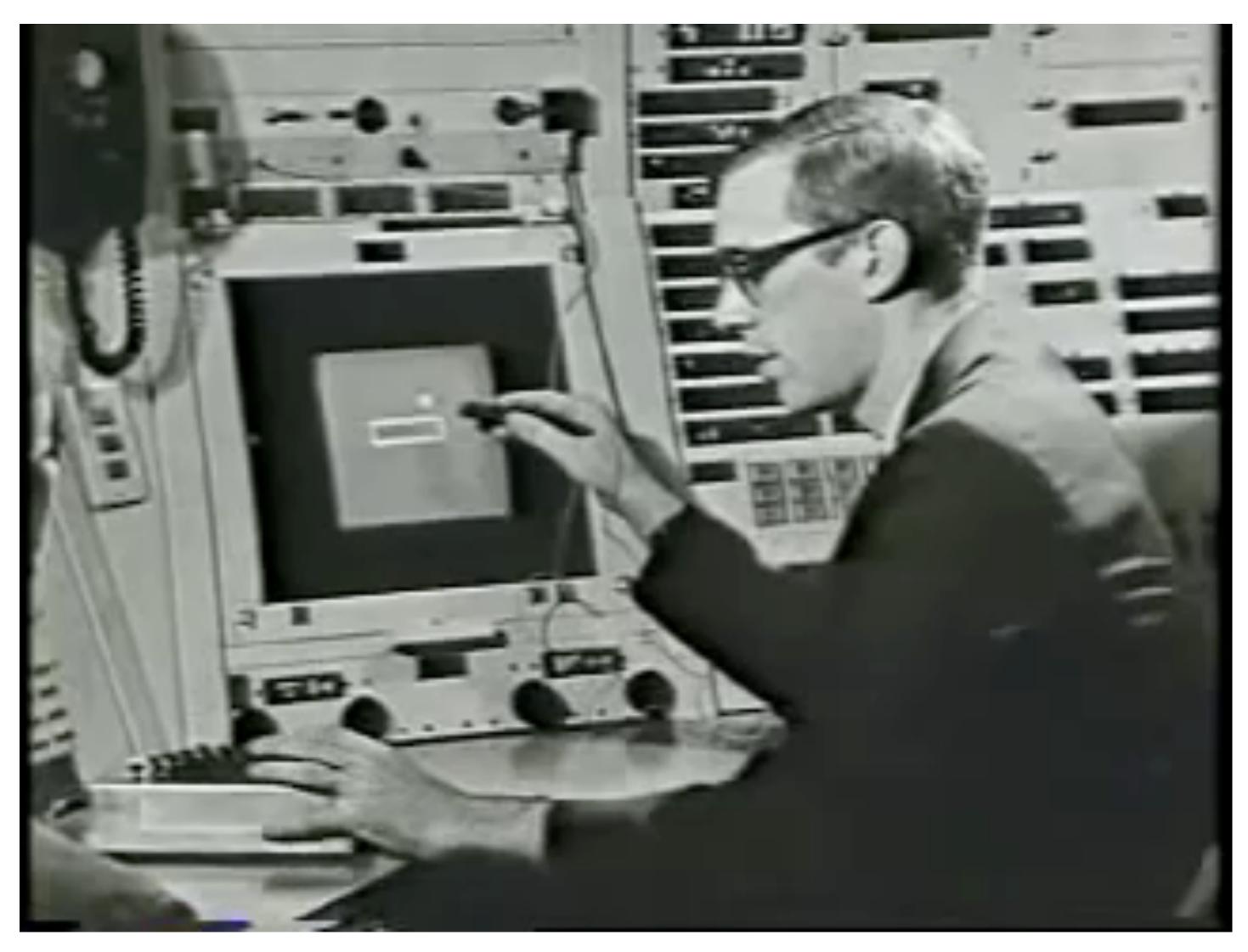
Interesting note: study commissioned by Leland Stanford (to determine if horse's feet ever off the ground)

First hand-drawn feature-length animation



Disney, "Snow White and the Seven Dwarfs" (1937)

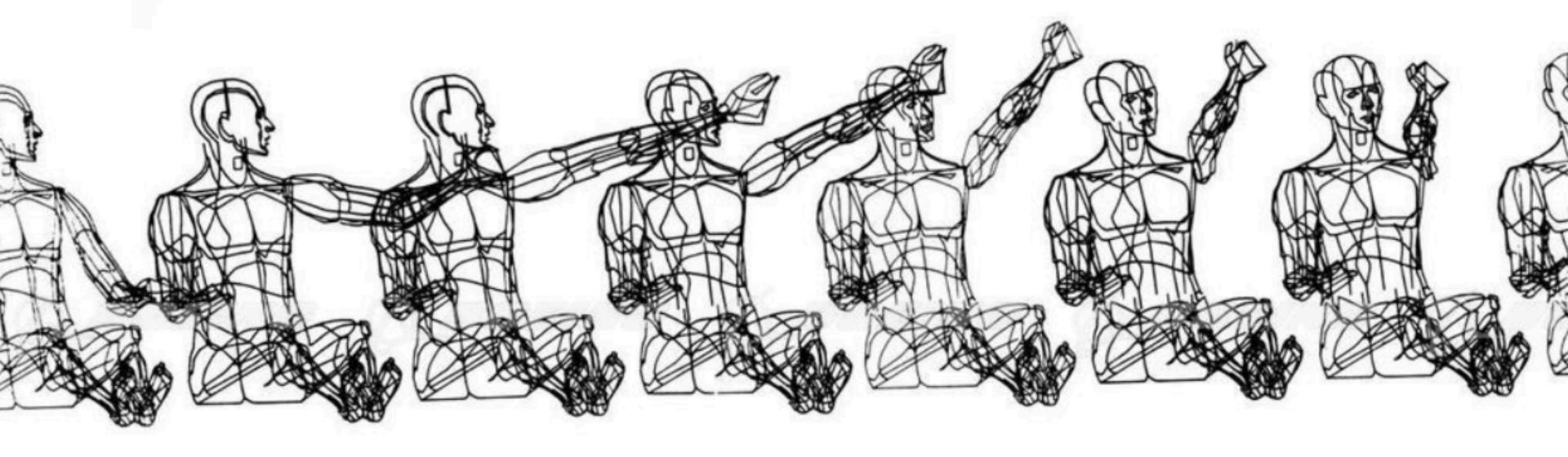
First digital-computer-generated animation



Ivan Sutherland, "Sketchpad" (1963)



First 3D computer animation



William Fetter, "Boeing Man" (1964)

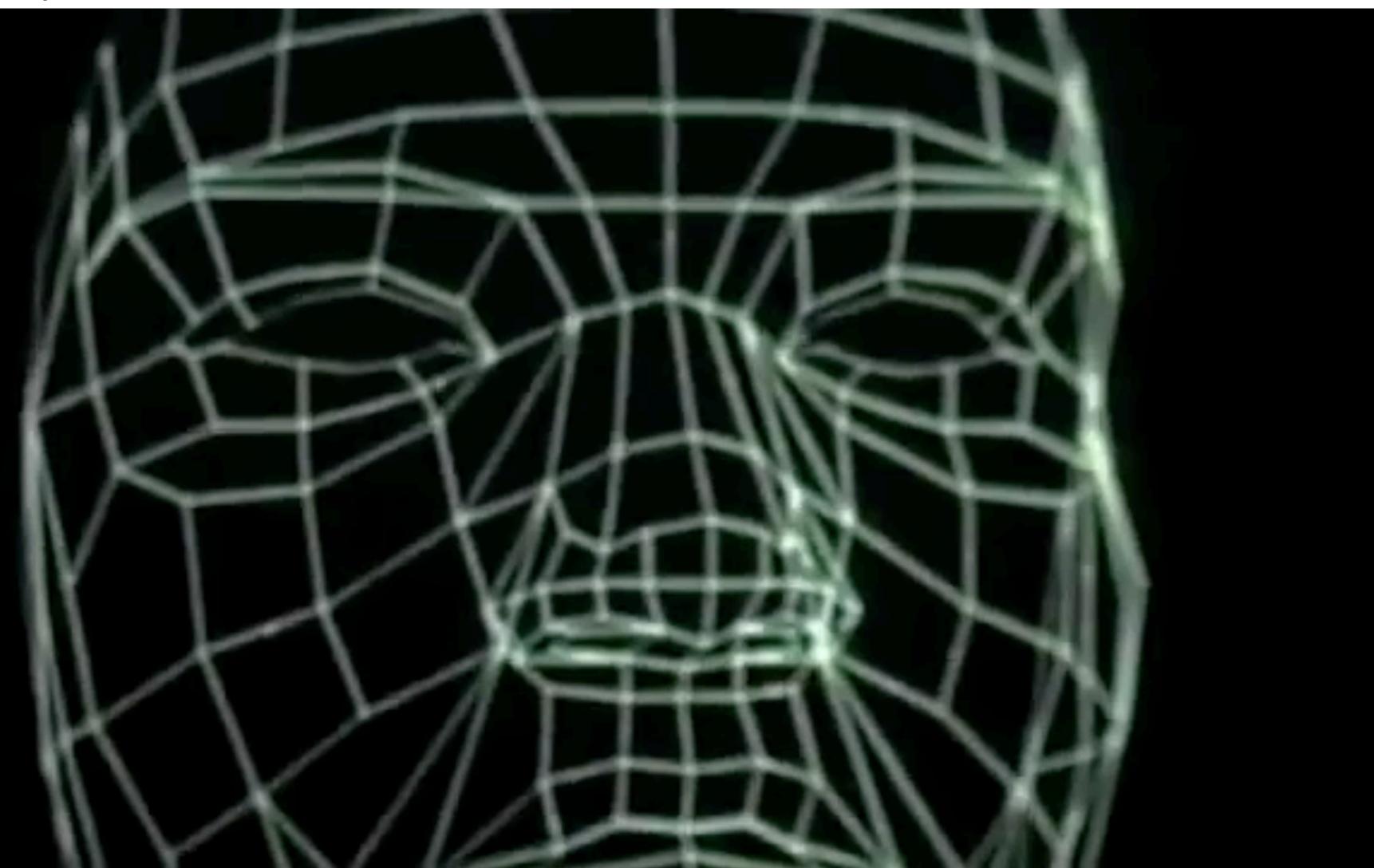
Early computer animation



Nikolay Konstantinov, "Kitty" (1968)

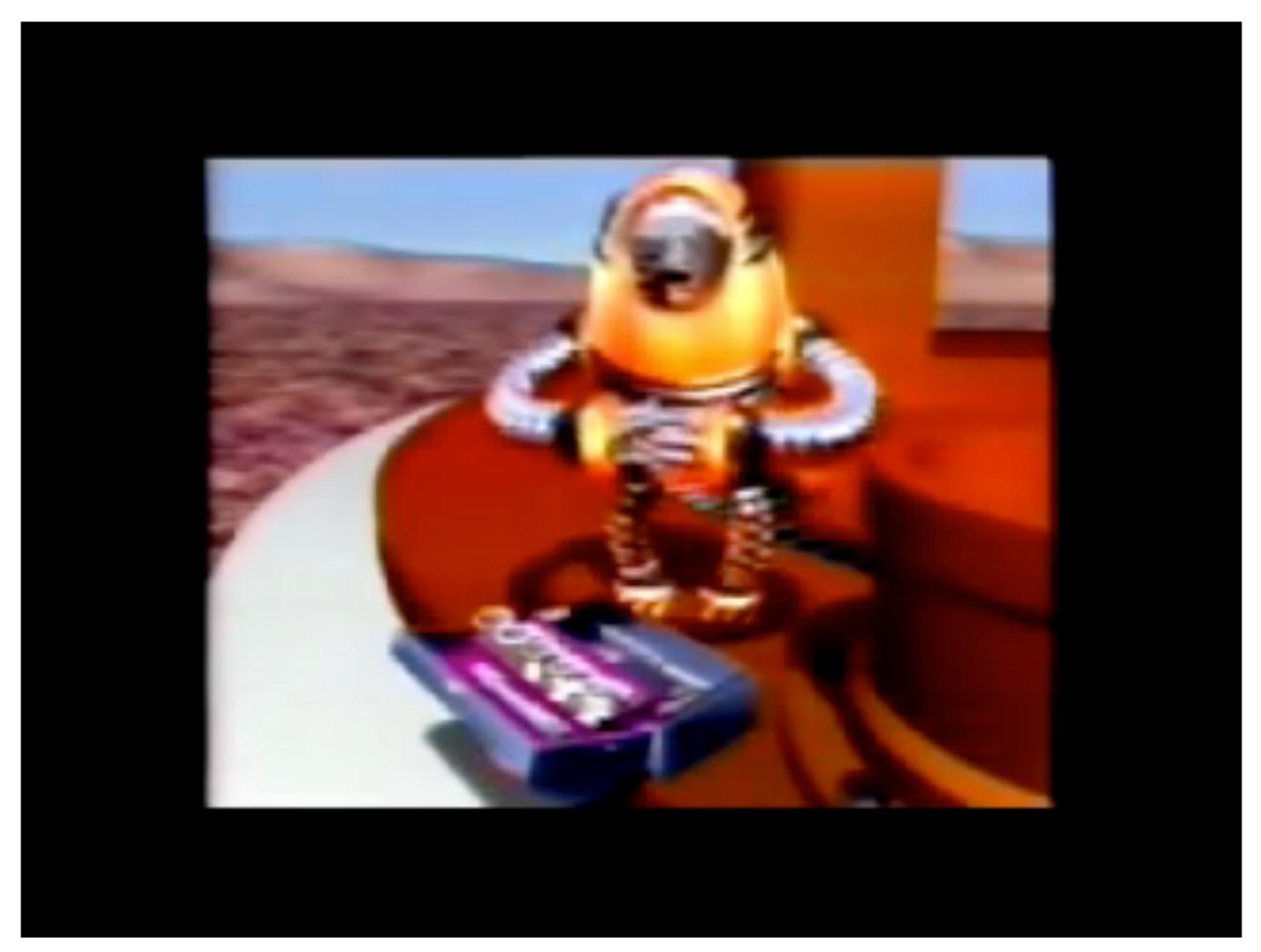


Early computer animation



Ed Catmull & Fred Park, "Computer Animated Faces" (1972)

First attempted CG feature film



NYIT [Williams, Heckbert, Catmull, ...], "The Works" (1984)



First CG feature film



Pixar, "Toy Story" (1995)

Computer animation - present day



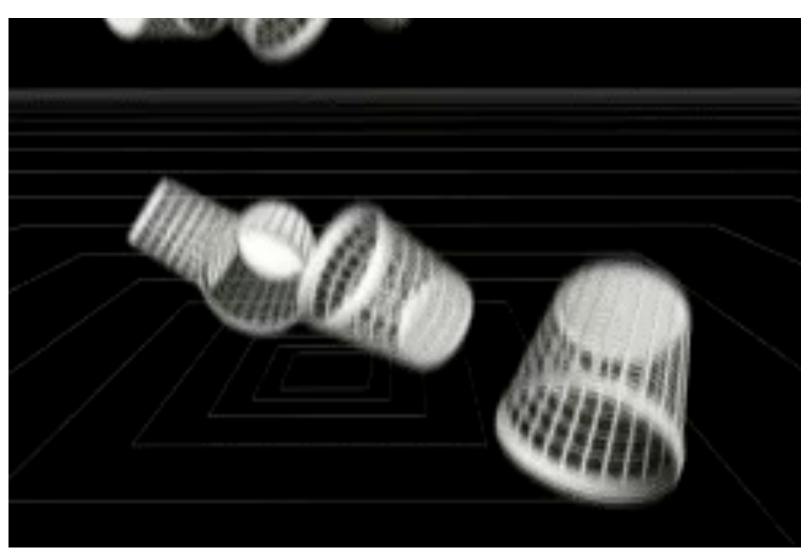
Notice combination of character animation, camera animation, and physical simulation in this clip. **Pixar's Coco (2017)** https://www.youtube.com/watch?v=GvicFasn_yM&t=4m5s

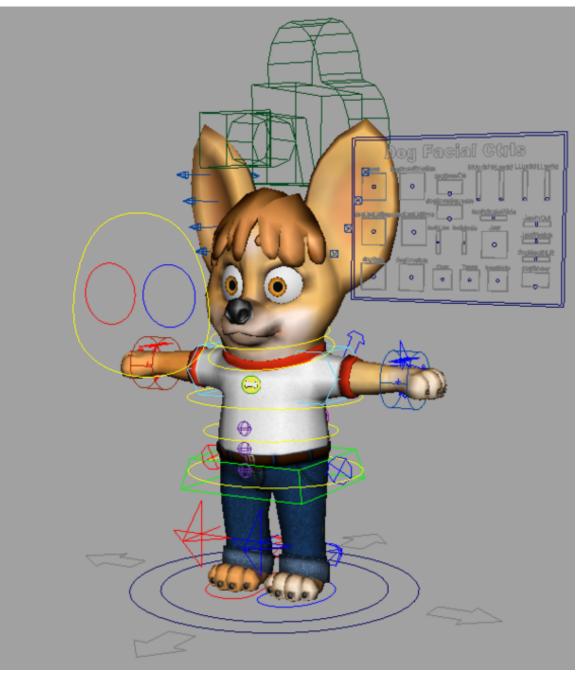
How do we describe motion on a computer?

Basic techniques in computer animation

- Artist-directed (e.g., keyframing)
- Data-driven (e.g., motion capture)
- Procedural (e.g., simulation)

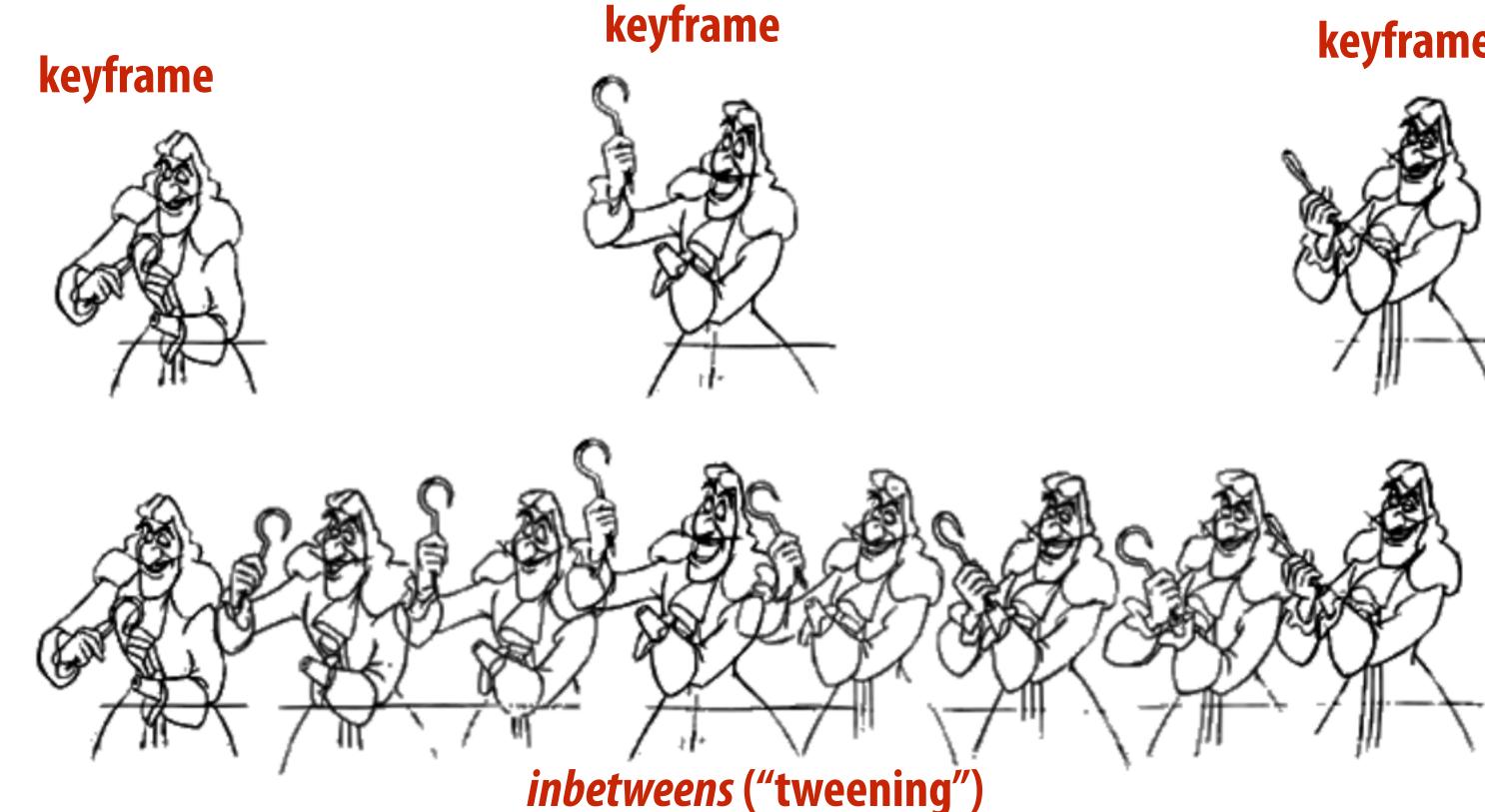






Generating motion (hand-drawn)

- Senior artist draws keyframes
- Assistant draws inbetweens
- **Tedious / labor intensive (opportunity for technology!)**

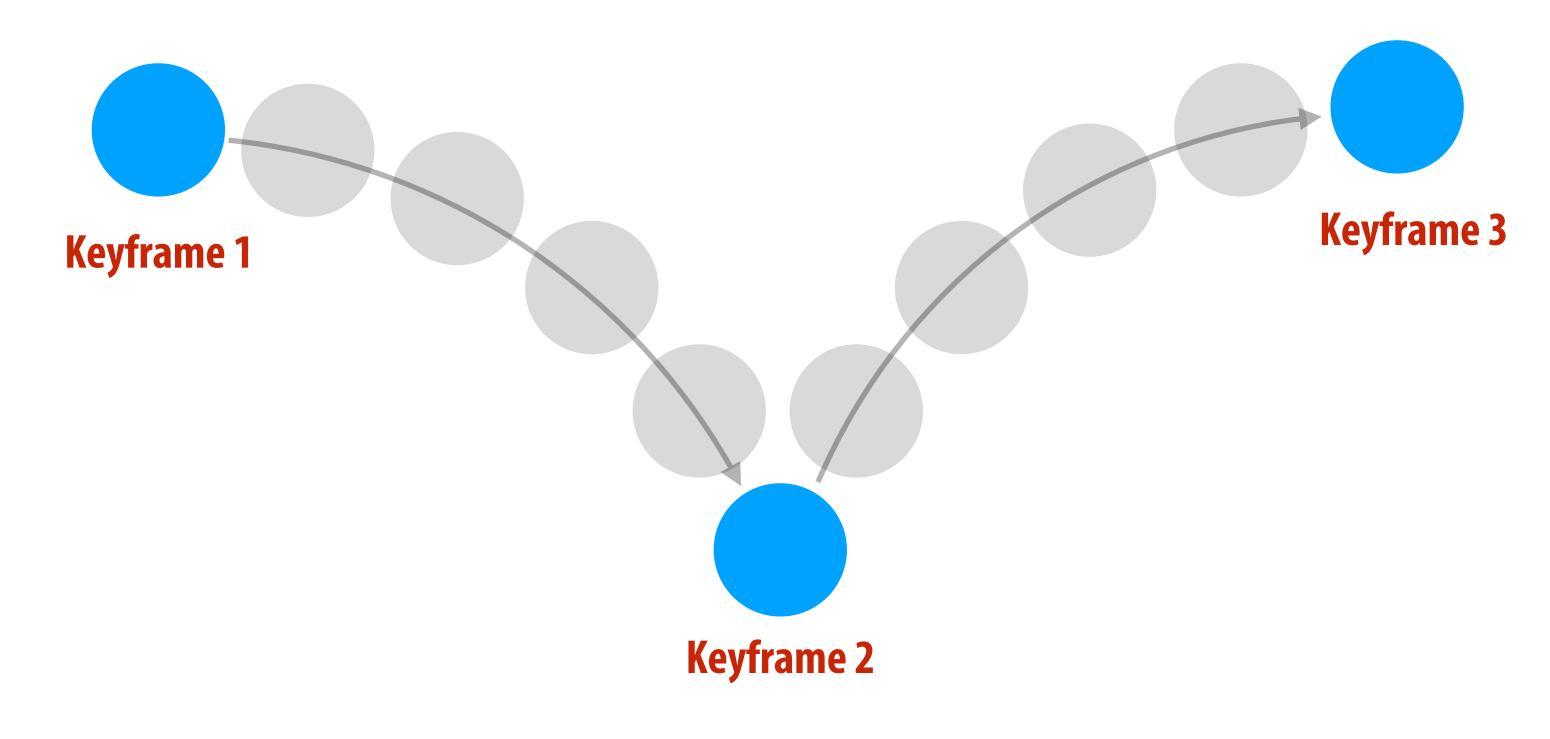


keyframe



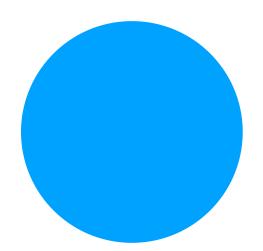
Keyframing

- **Basic idea:**
 - Animator specifies important events only
 - Computer fills in the rest via interpolation/approximation
 - "Events" don't have to be position
- Could be color, light intensity, camera zoom, ...

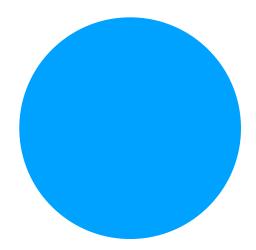




Keyframing example

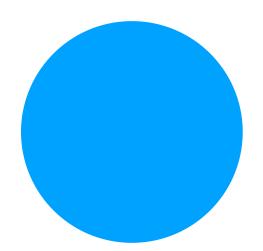


Keyframe 1

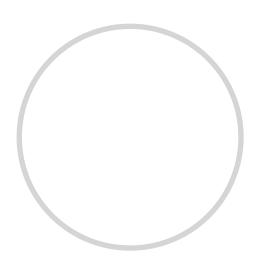


Keyframe 2

Keyframing example

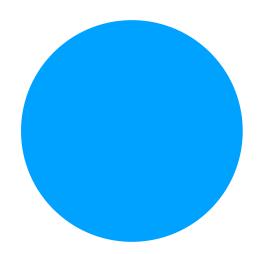


Keyframe 1



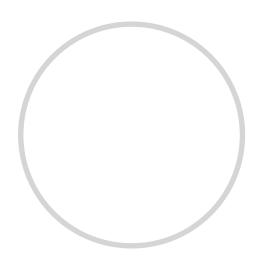
Keyframe 2

Keyframing example



Keyframe 1



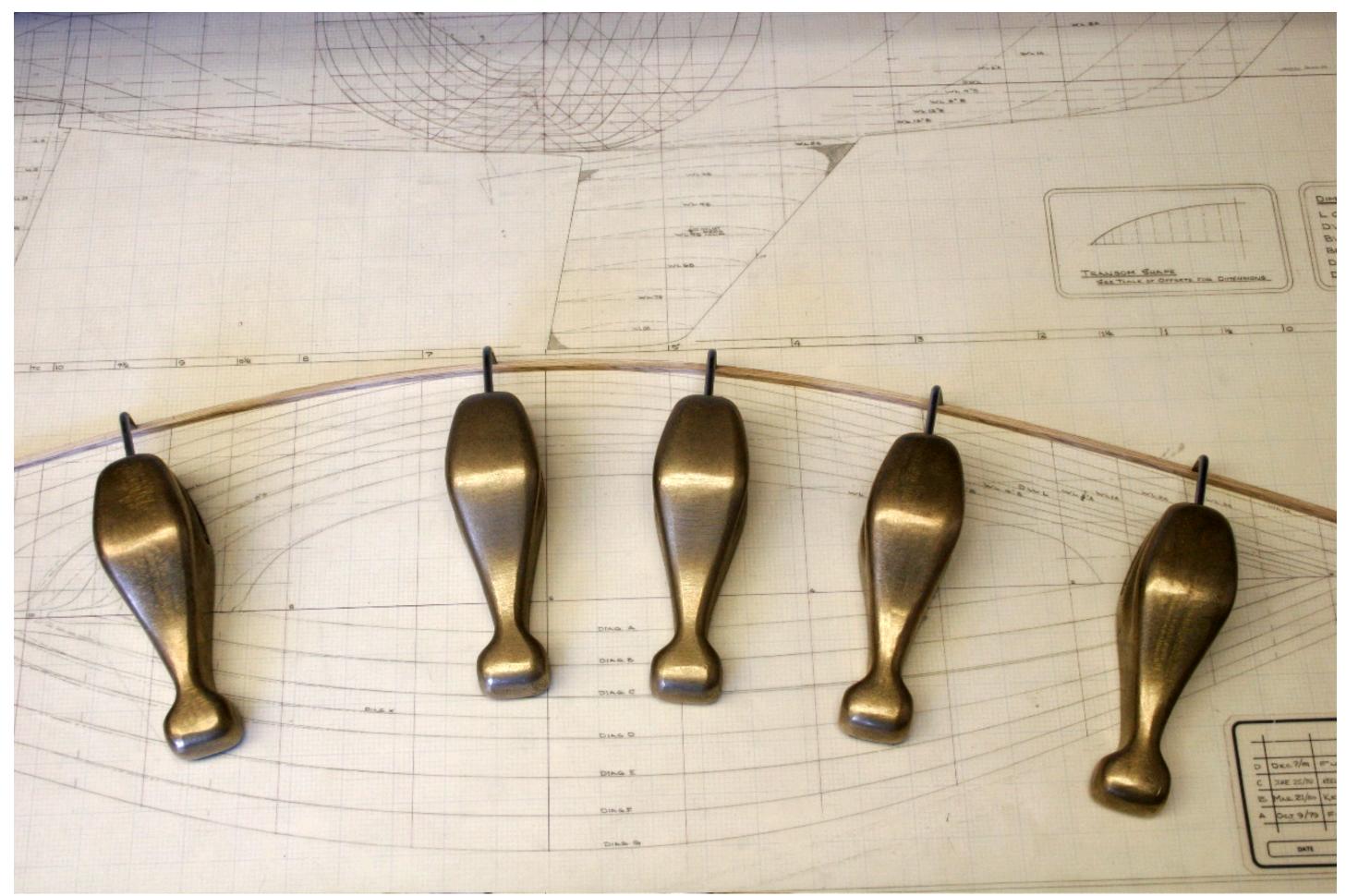


Keyframe 3

How do we interpolate data?

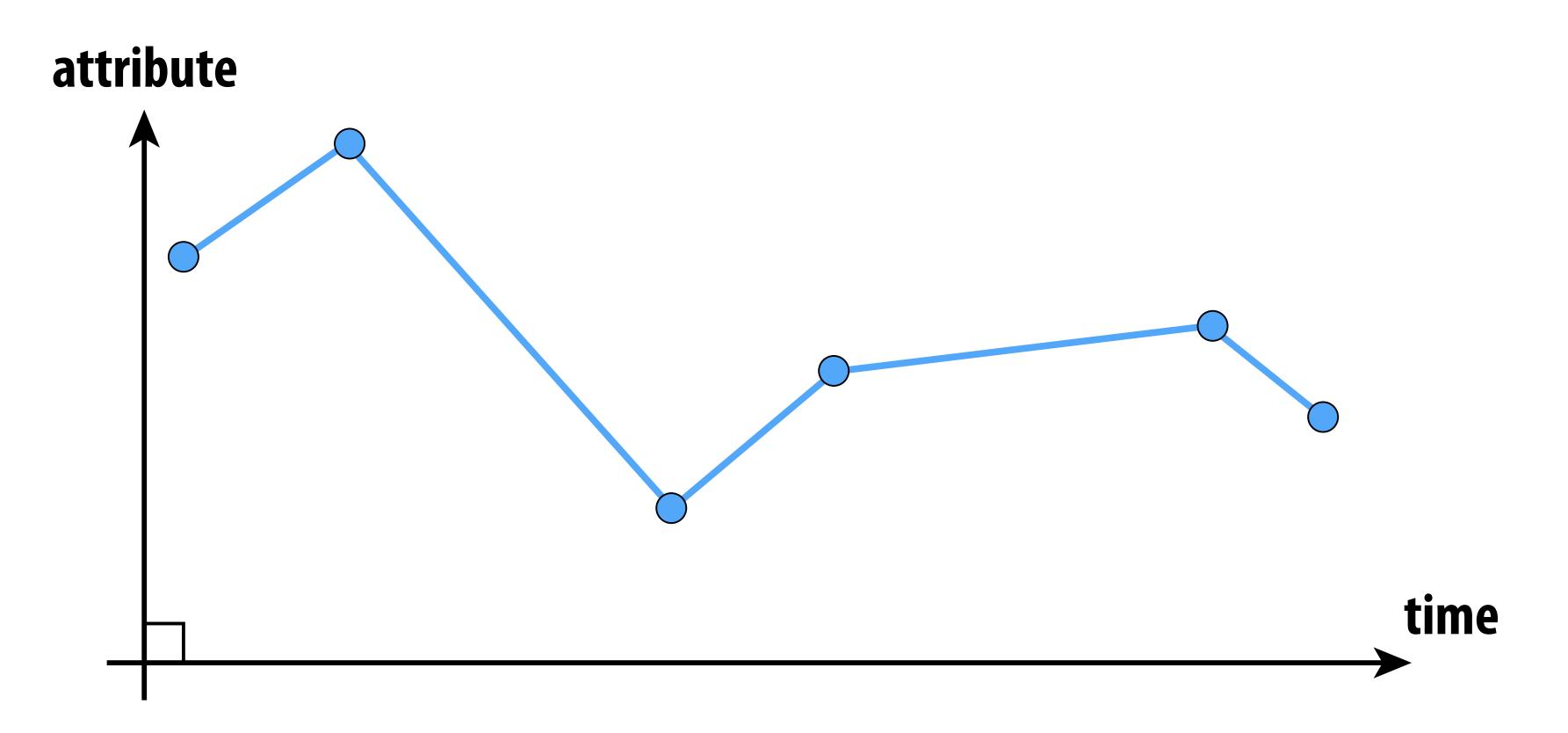
Spline interpolation

Mathematical theory of interpolation arose from study of thin strips of wood or metal ("splines") under various forces

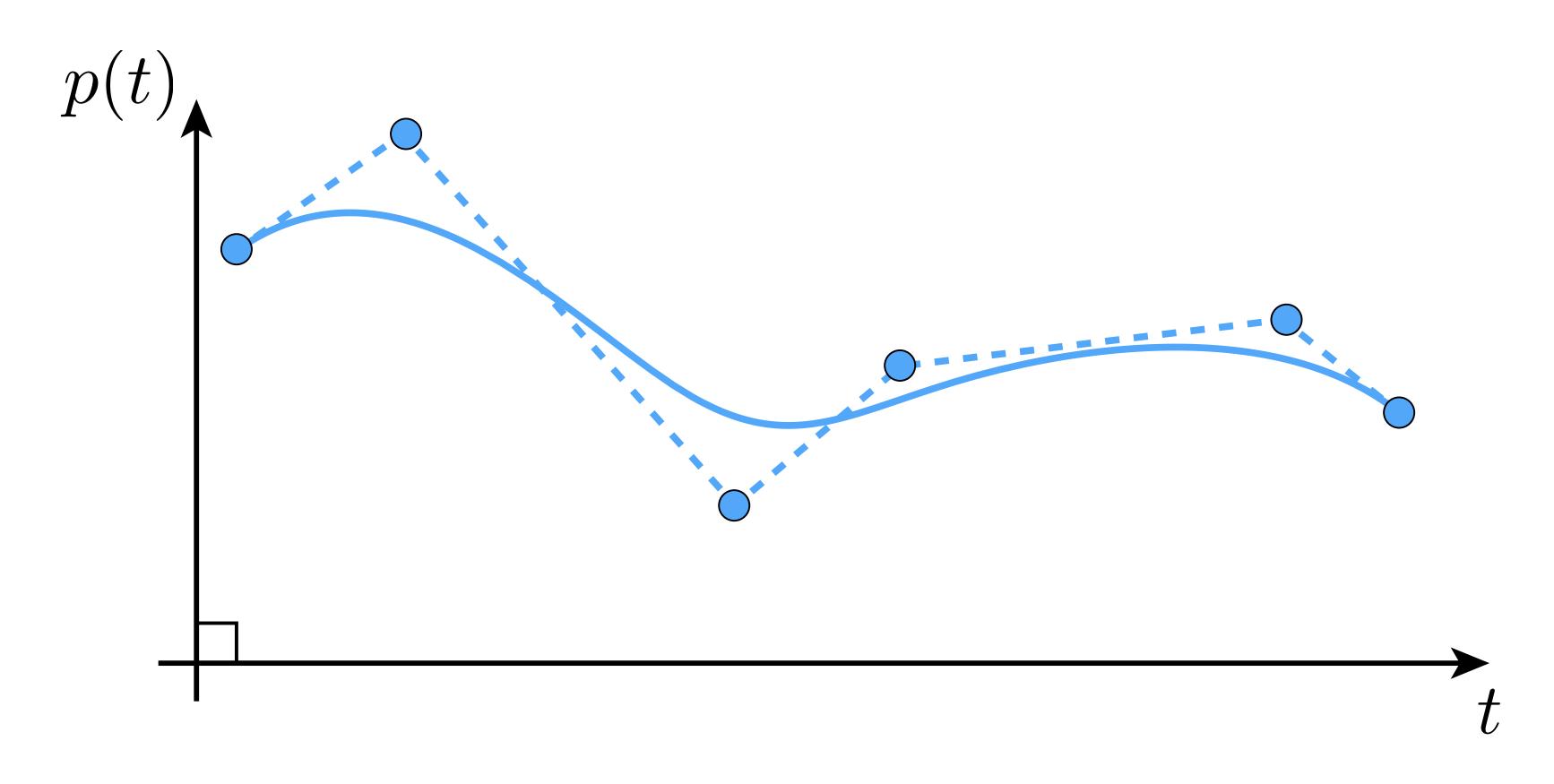


Interpolation

- **Basic idea: "connect the dots"**
- E.g., piecewise linear interpolation
- Simple, but yields "rough" motion (infinite acceleration)



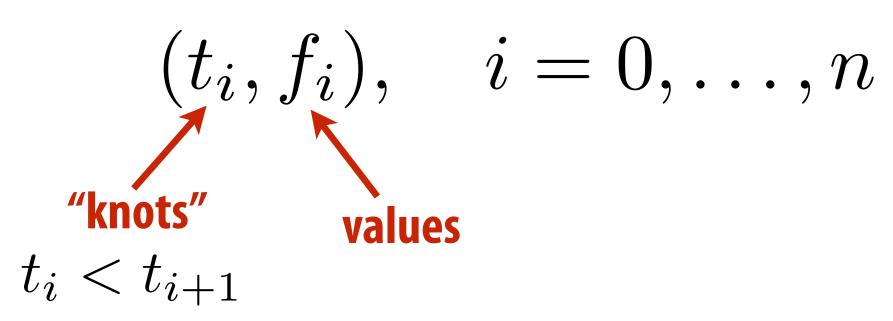
Piecewise polynomial interpolation Common interpolant: piecewise polynomial "spline"



Basic motivation: get better continuity than piecewise linear!

Splines

- In general, a *spline* is any piecewise polynomial function
- In 1D, spline interpolates data over the real line:



"Interpolates" means that the function *exactly* passes through those values:

$$f(t_i) = f_i \quad \forall i$$

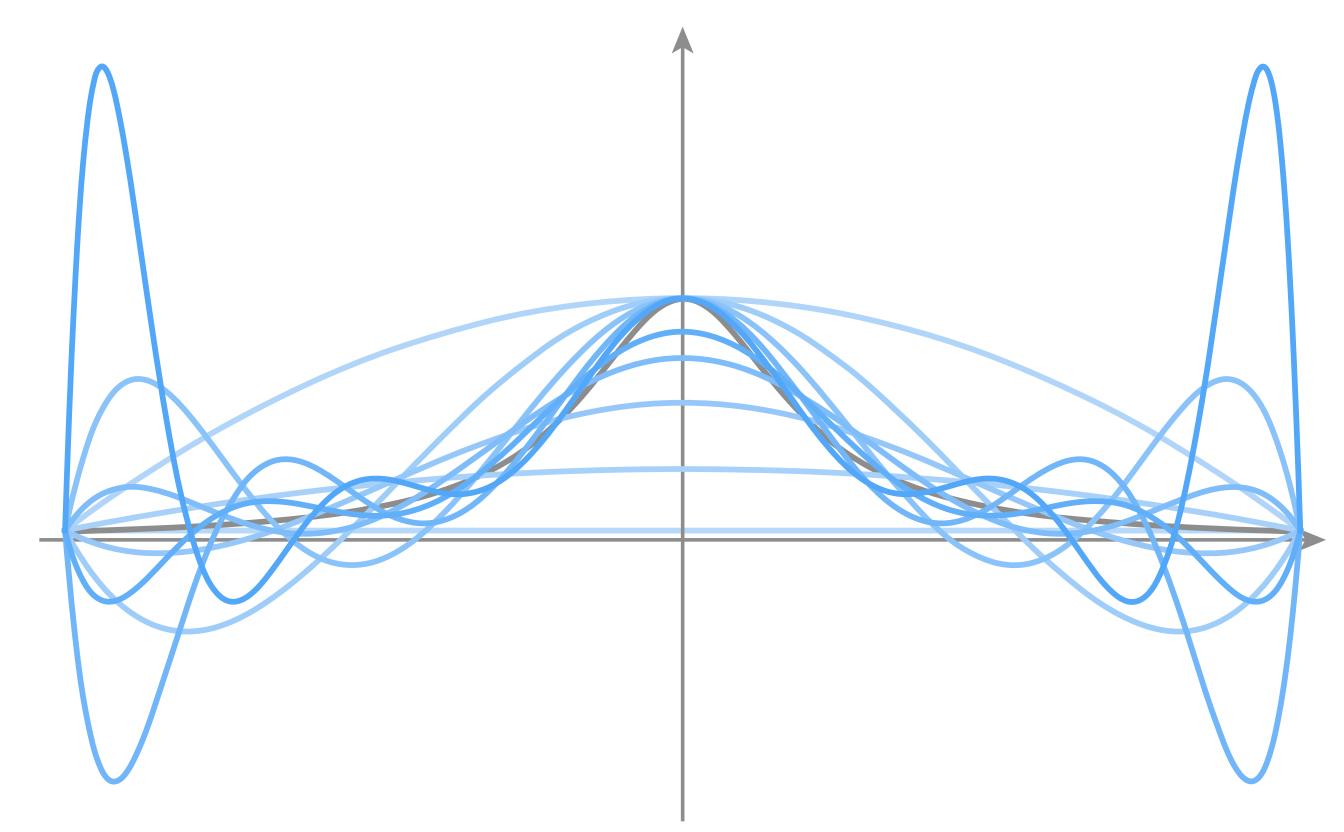
The only other condition is that the function is a *polynomial* when restricted to any interval between knots:

for
$$t_i \leq t \leq t_{i+1}, f(t) = \sum_{i=1}^{d} \sum_{i=1}^{d$$

polynomial **degree** $\sum_{j=1}^{} c_j t^j =: p_i(t)$

What's so special about *cubic* polynomials? Splines most commonly used for interpolation are *cubic* (d=3)

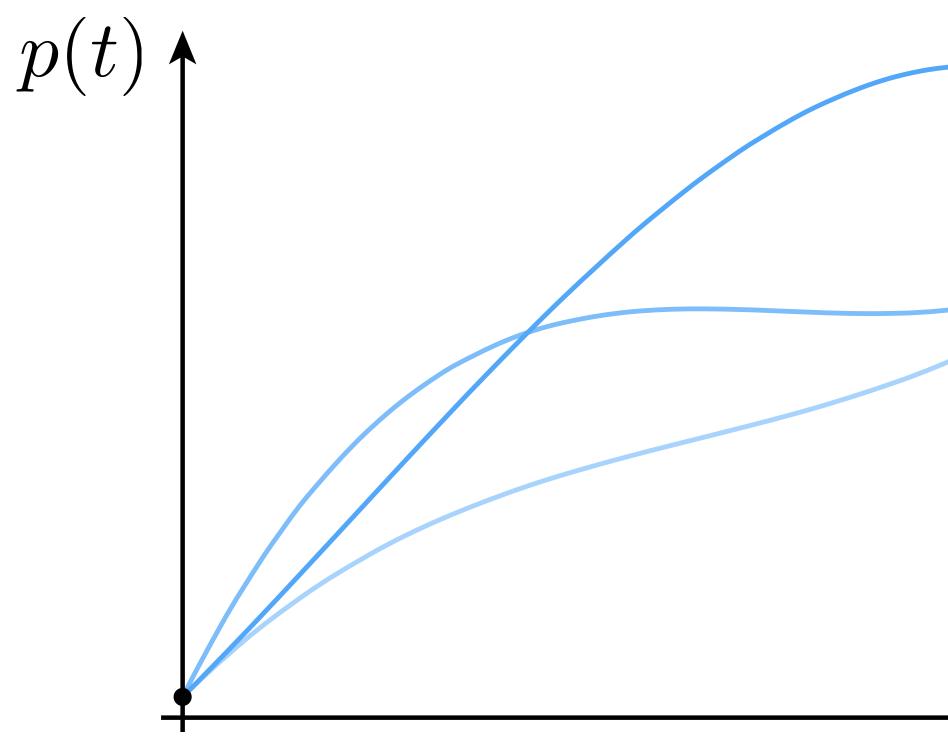
- **Can provide "reasonable" continuity**
- Tempting to use higher-degree polynomials to get higher-order continuity
- Can lead to oscillation, ultimately worse approximation:



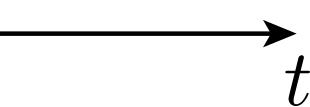
Fitting a cubic polynomial to endpoints

Consider a *single* cubic polynomial $p(t) = at^3 + bt^2 + ct + d$

Suppose we want it to match two given endpoints:



Many solutions!

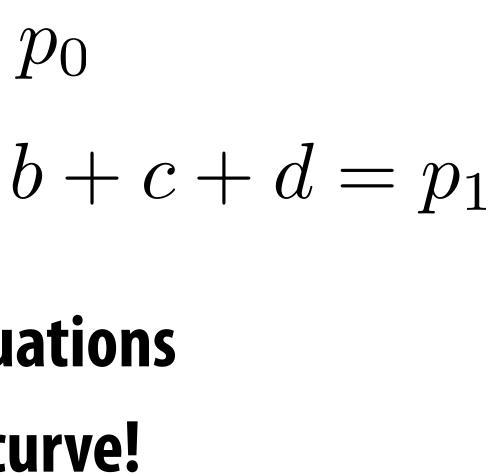


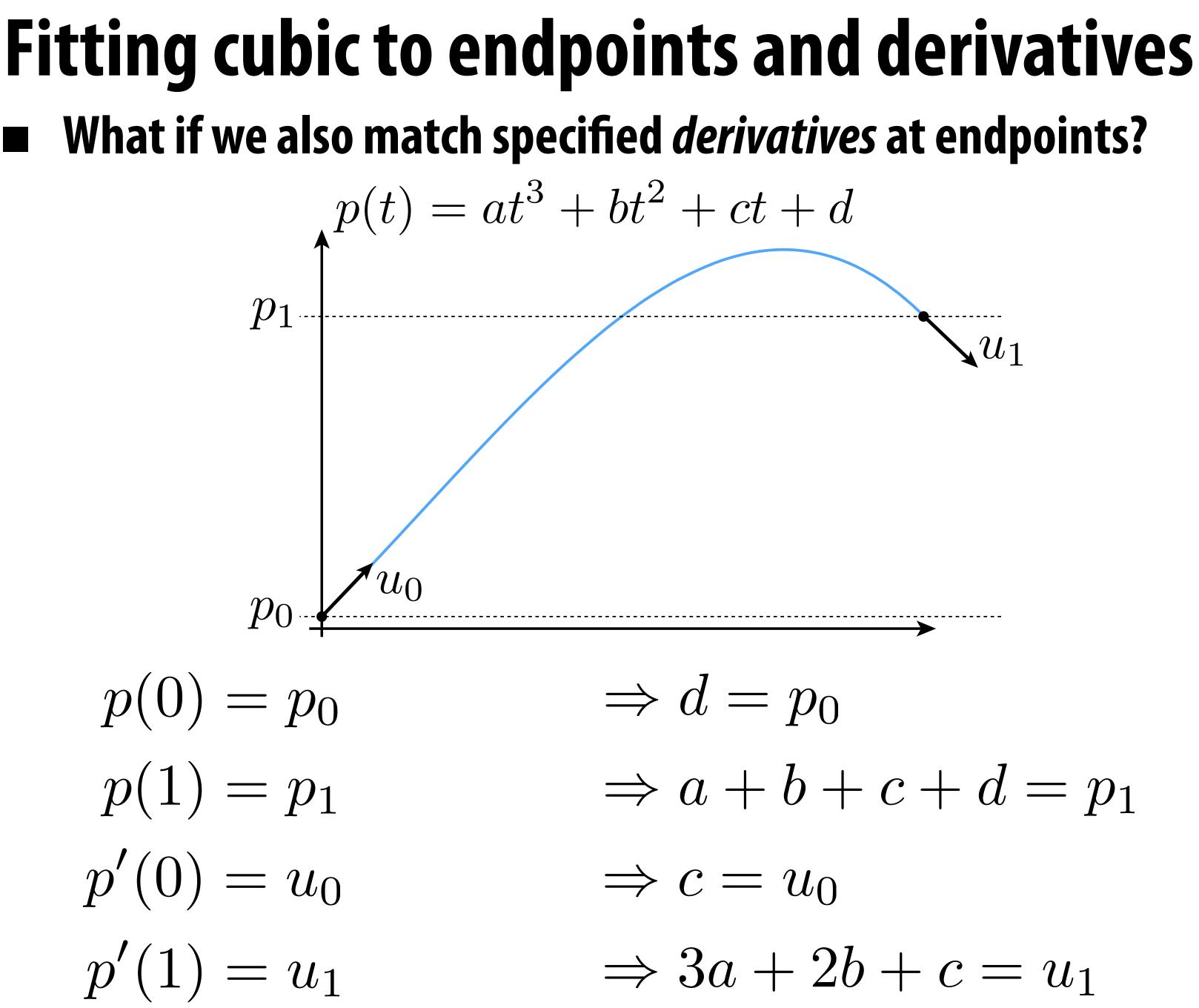
Cubic polynomial - degrees of freedom

- Why are there so many different solutions?
- Cubic polynomial has four *degrees of freedom (DOFs)*, namely four coefficients (a,b,c,d) that we can manipulate/control
- Only need *two* degrees of freedom to specify endpoints:

$$p(t) = at^{3} + bt^{2} + ct + d$$
$$p(0) = p_{0} \qquad \Rightarrow d =$$
$$p(1) = p_{1} \qquad \Rightarrow a + d$$

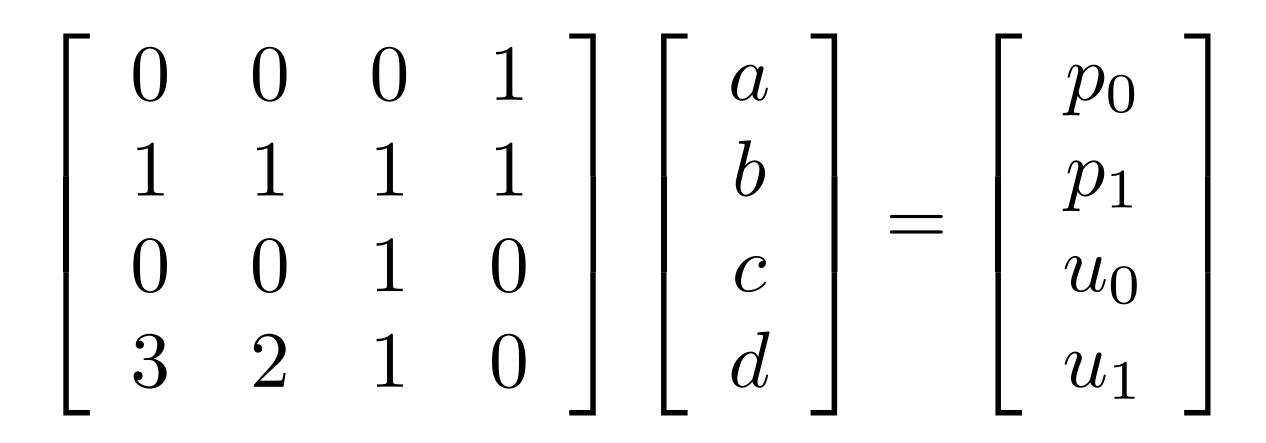
Overall, four unknowns but only *two* **equations** Not enough to uniquely determine the curve!



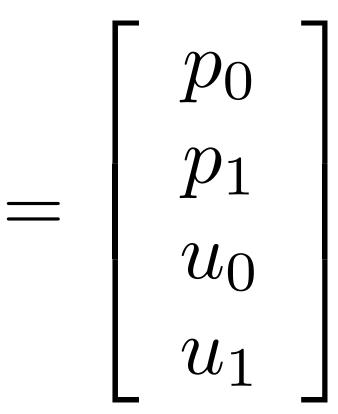


Splines as linear systems

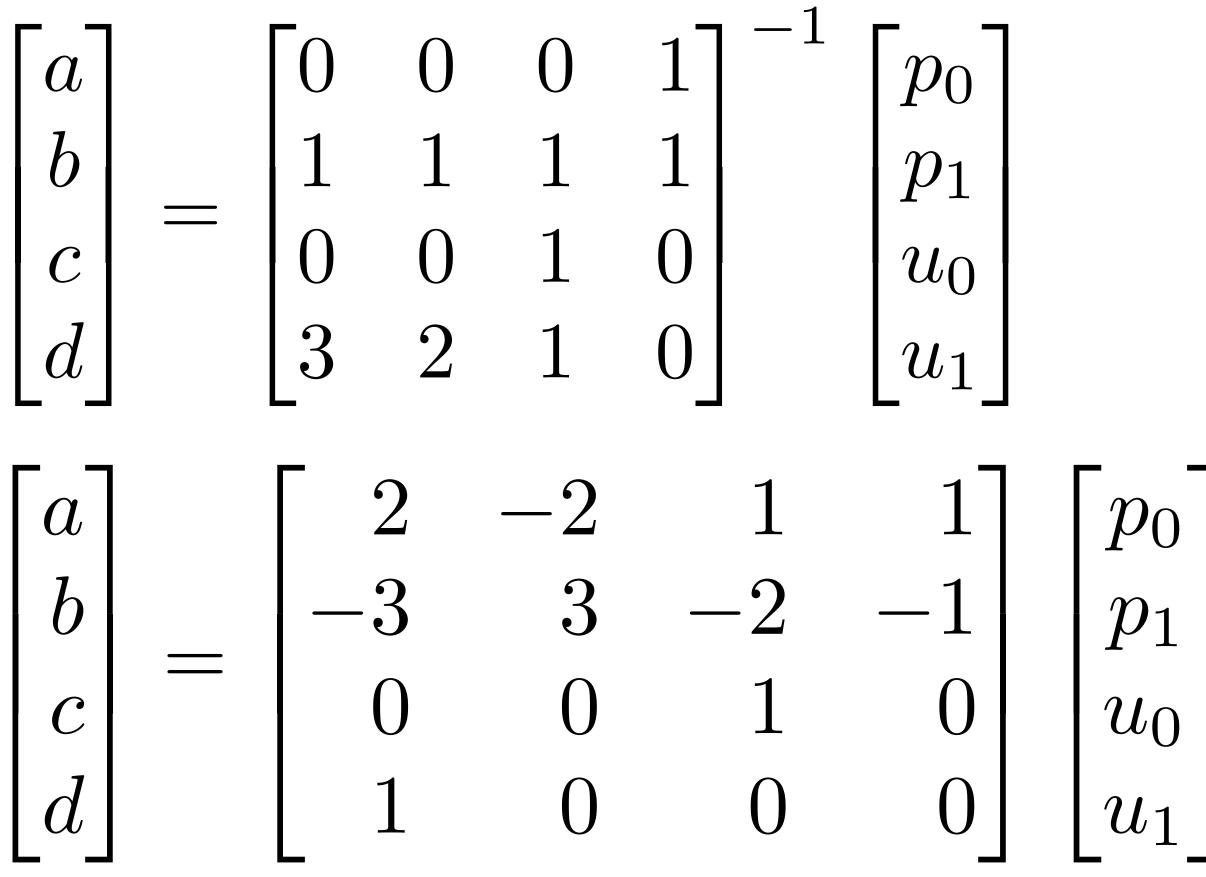
- Now we have four equations and four unknowns
- **Could also express as a matrix equation:**



- This is a common way to define a spline
 - Each condition on spline leads to a linear equality
 - Hence, if we have m degrees of freedom, we need m (linearly independent!) conditions to determine spline



Solve for polynomial coefficients



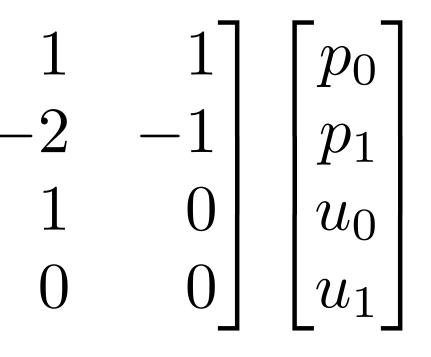
Matrix form

Interpolates endpoints, matches derivatives

$$p(t) = at^3 + bt^2 + ct + d$$

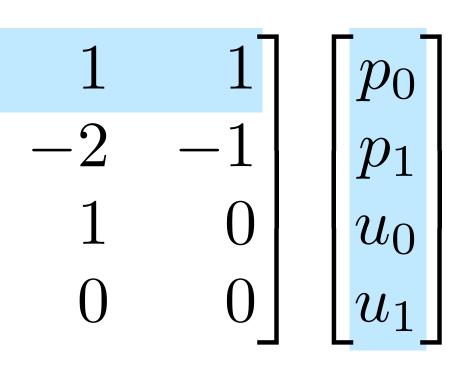
 $p(t) = \begin{bmatrix} t^3 & t^2 & t & 1 \end{bmatrix} \begin{vmatrix} a \\ b \\ c \\ d \end{vmatrix}$

 $= \begin{bmatrix} t^3 & t^2 & t & 1 \end{bmatrix} \begin{bmatrix} 2 & -2 & 1 & 1 \\ -3 & 3 & -2 & -1 \\ 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} p_0 \\ p_1 \\ u_0 \\ u_1 \end{bmatrix}$



Interpretation 1: matrix rows = coefficient formulas

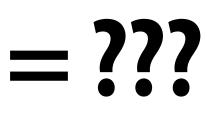
$$p(t) = at^{3} + bt^{2} + ct + d$$
$$= \begin{bmatrix} t^{3} & t^{2} & t & 1 \end{bmatrix} \begin{bmatrix} 2 & -2 \\ -3 & 3 \\ 0 & 0 \\ 1 & 0 \end{bmatrix}$$



Interpretation 2: matrix cols = ???

$$p(t) = at^{3} + bt^{2} + ct + d$$
$$= \begin{bmatrix} t^{3} & t^{2} & t & 1 \end{bmatrix} \begin{bmatrix} 2 & -2 \\ -3 & 3 \\ 0 & 0 \\ 1 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 2t^{3} - 3t^{2} + 1 \\ -2t^{3} + 3t^{2} \\ t^{3} - 2t^{2} + t \\ t^{3} - t^{2} \end{bmatrix}^{T} \begin{bmatrix} p_{0} \\ p_{1} \\ u_{0} \\ u_{1} \end{bmatrix}$$



$\begin{array}{cccc} 1 & 1 \\ -2 & -1 \\ 1 & 0 \\ 0 & 0 \end{array} \begin{bmatrix} p_0 \\ p_1 \\ u_0 \\ u_1 \end{bmatrix}$

Hermite basis functions

$$p(t) = \begin{bmatrix} t^3 & t^2 & t & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = \begin{bmatrix} H_0(t) & H_1(t) & H_2(t) & H_3(t) \end{bmatrix} \begin{bmatrix} p_0 \\ p_1 \\ u_0 \\ u_1 \end{bmatrix}$$

One common basis for cubic polynomials

Hermite Basis for cubic polynomials

 $f_0(t) = t^3$ $H_0(t) = 2$ $f_1(t) = t^2$ $H_1(t) = H_2(t) = t^3 - 2t^2 + t$ $f_2(t) = t$ $H_3(t) = t^3 - t^2$ $f_3(t) = 1$

Either basis can represent a cubic polynomial through linear combination!

$$2t^3 - 3t^2 + 1$$

 $-2t^3 + 3t^2$

Natural splines

- Now consider *piecewise* spline made of *n* cubic polynomials *p_i*
- For each interval, want polynomial "piece" p_i to interpolate data (e.g., keyframes) at both endpoints: $p_i(t_i) = f_i, \ p_i(t_{i+1}) = f_{i+1}, \ i = 0, \dots, n-1$
- Want tangents to agree at endpoints ("C¹ continuity"): $p'_{i}(t_{i+1}) = p'_{i+1}(t_{i+1}), \ i = 0, \dots, n-2$
- Also want curvature to agree at endpoints ("C² continuity"): $p''_i(t_{i+1}) = p''_{i+1}(t_{i+1}), i = 0, ..., n-2$
- How many equations do we have at this point?
 - 2n+(n-1)+(n-1) = 4n-2
- Pin down remaining DOFs by setting 2nd derivative (curvature) to zero at endpoints

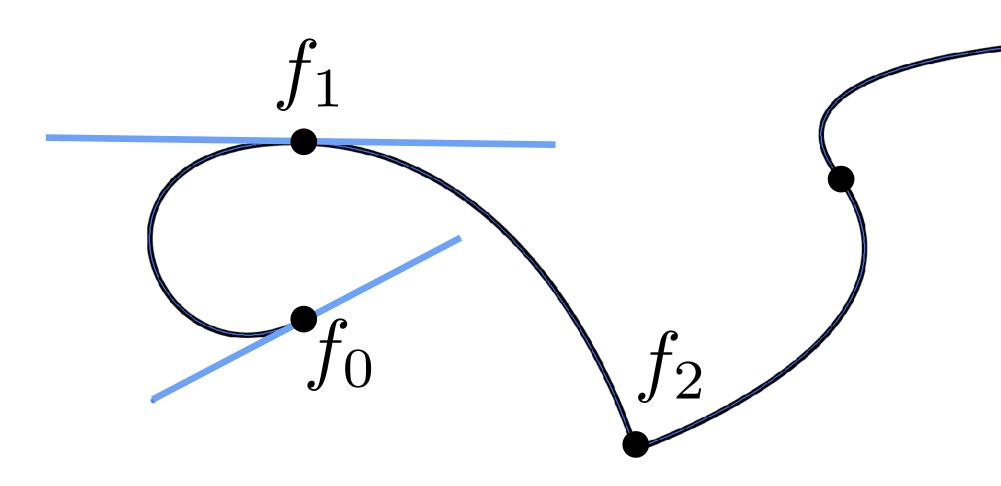
Spline desiderata

In general, what are some properties of a "good" spline?

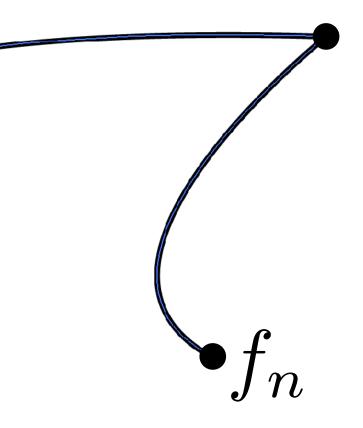
- INTERPOLATION: spline passes *exactly* through data points
- CONTINUITY: at least *twice* differentiable everywhere (for animation = constant "acceleration")
- LOCALITY: moving one control point doesn't affect whole curve
- How does our natural spline do?
 - INTERPOLATION: yes, by construction
 - CONTINUITY: C² everywhere, by construction
 - LOCALITY: no, coefficients depend on global linear system
- Many other types of splines we can consider
- Spoiler: there is "no free lunch" with cubic splines (can't simultaneously get all three properties)

Back to Hermite splines from earlier in lecture

Hermite: each cubic "piece" specified by endpoints and tangents:



- **Commonly used for 2D vector art (Illustrator, Inkscape, SVG, ...)**
- **Can we get tangent (C1) continuity?**
- Sure: set both tangents to same value on both sides of knot! **E.g.**, f_1 above, but not f_2



Recall from geometry lecture: Bézier curves

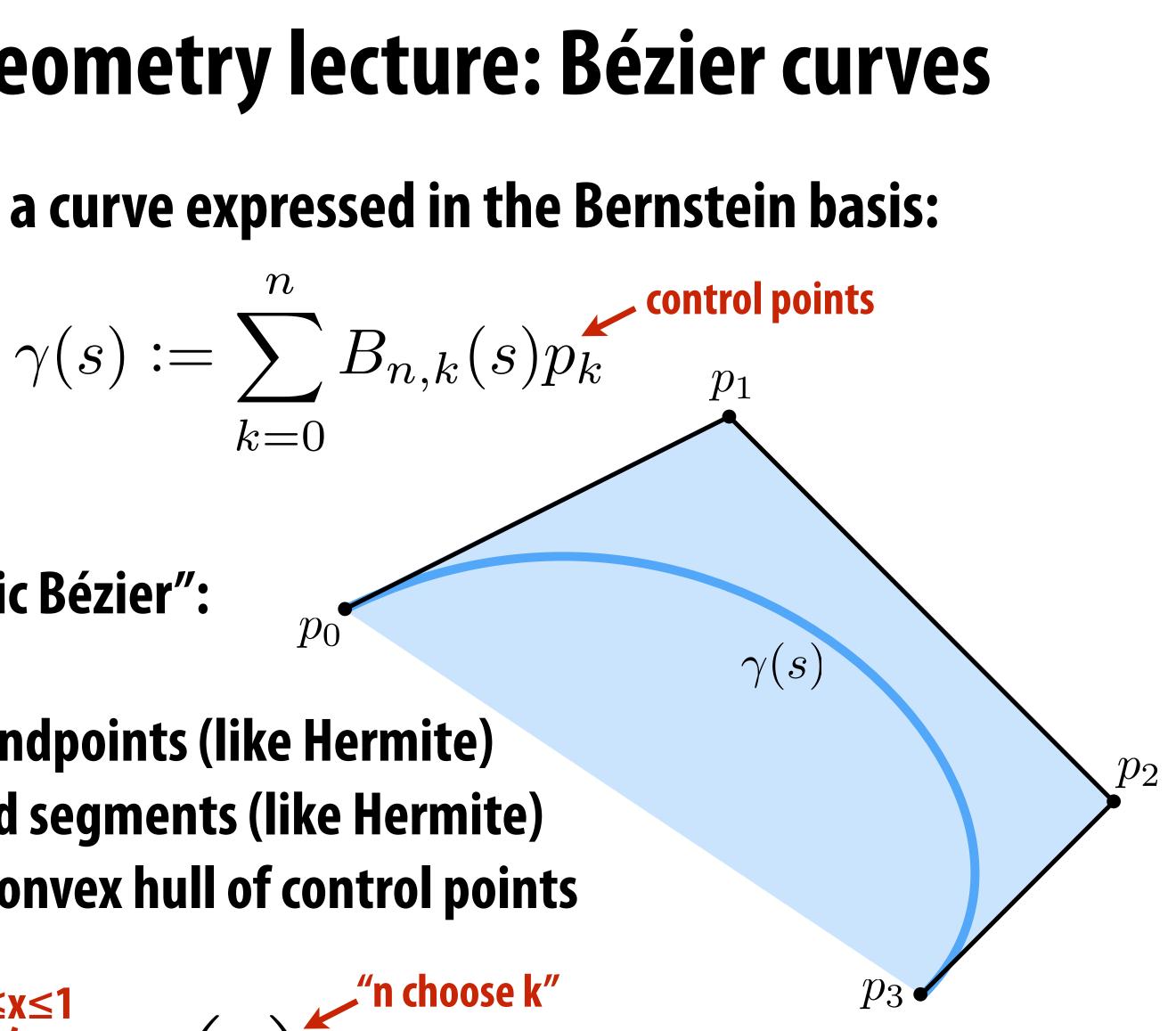
A Bézier curve is a curve expressed in the Bernstein basis:

- For n=3, get "cubic Bézier":
- **Properties:**
 - 1. interpolates endpoints (like Hermite)
 - 2. tangent to end segments (like Hermite)
 - 3. contained in convex hull of control points

$$\begin{array}{c} \text{degree} \\ 0 \leq x \leq 1 \\ B_k^n(x) := \binom{n}{k} x^k (1 - k) \\ k = 0, \dots, n \end{array}$$

k = 0

 p_0



 $x)^{n-k}$

Properties of Hermite/Bézier spline

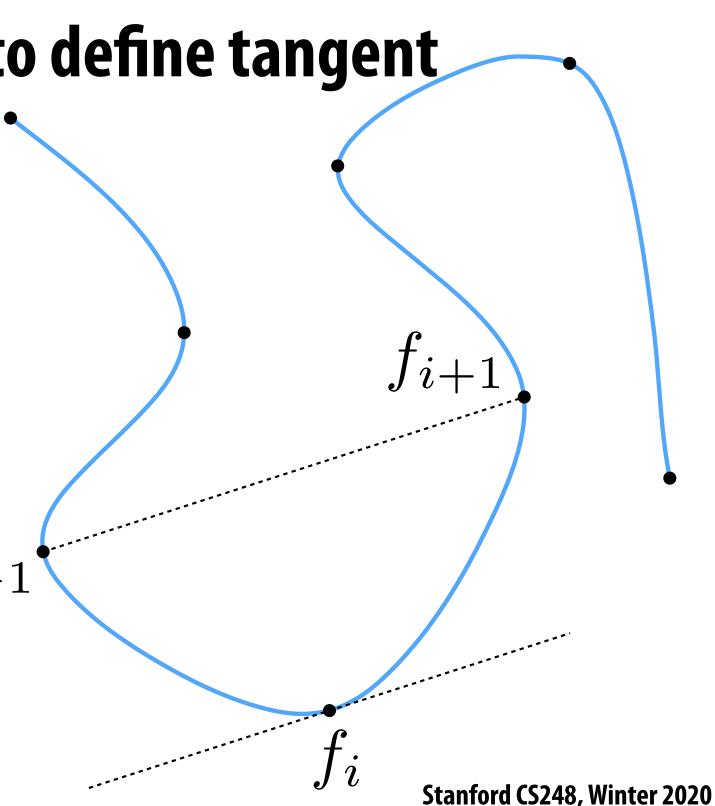
- More precisely, want endpoints to interpolate data: $p_i(t_i) = f_i, \ p_i(t_{i+1}) = f_{i+1}, \ i = 0, \dots, n-1$
- Also want tangents to interpolate some given data: $p'_{i}(t_{i}) = u_{i}, \ p'_{i}(t_{i+1}) = u_{i+1}, \ i = 0, i, ..., n-1$
- How is this *different* from our natural spline's tangent condition?
- There, tangents didn't have to match any prescribed value— they merely had to be the same. Here, they are given.
- How many conditions overall?

 $\square 2n + 2n = 4n$

- What properties does this curve have?
 - **INTERPOLATION and LOCALITY, but not C² CONTINUITY**

Catmull-Rom splines

- Sometimes makes sense to specify tangents (e.g., illustration)
- **Often more convenient to just specify** *values*
- **Catmull-Rom: specialization of Hermite spline, determined** by values alone
- **Basic idea: use difference of neighbors to define tangent** $u_i := \frac{f_{i+1} - f_{i-1}}{t_{i+1} - t_{i-1}}$
- All the same properties as any other Hermite spline (locality, etc.)
- **Commonly used to interpolate** motion in computer animation.
- Many, many variants, but Catmull-Rom is usually good starting point



Spline desiderata, revisited

	INTERPOLATION	CONTINUITY	LOCALITY
natural	YES	YES	NO
Hermite	YES	NO	YES
???	NO	YES	YES
See B-Splines			

But what quantities do we seek to interpolate?

Simple example: camera path

- Animate position, direction, "up" direction of camera
 - each path is a function f(t) = (x(t), y(t), z(t))
 - each component (x,y,z) is a spline



h ion of camera t), z(t))

Zaha Hadid Architects—City of Dreams Hotel Towe

Character animation

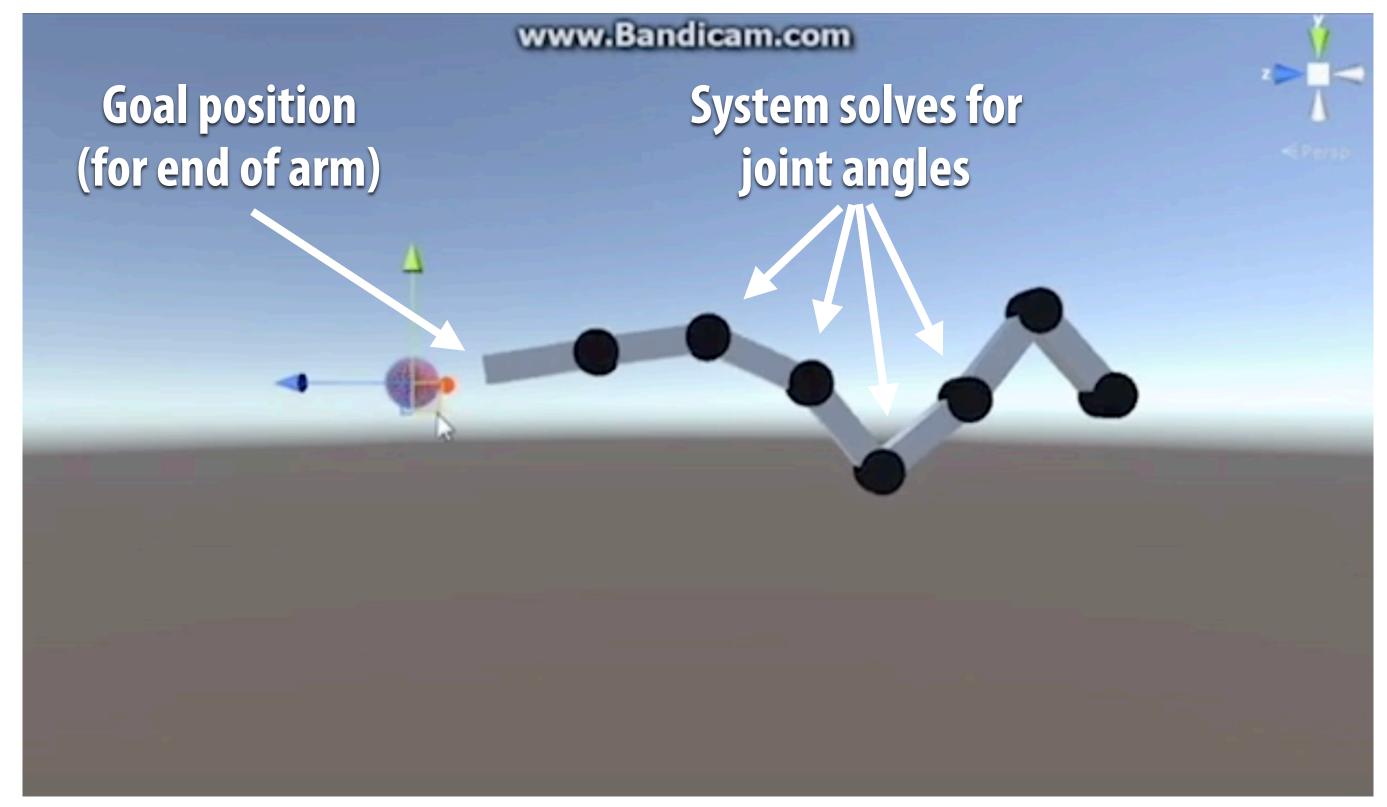
- Scene graph/kinematic chain: scene as tree of transformations
- E.g. in our "cube person," configuration of a leg might be expressed as rotation relative to body
- **Often have sophisticated "rig":**



Even w/ computer "tweening," its a lot of work to animate!

Inverse kinematics

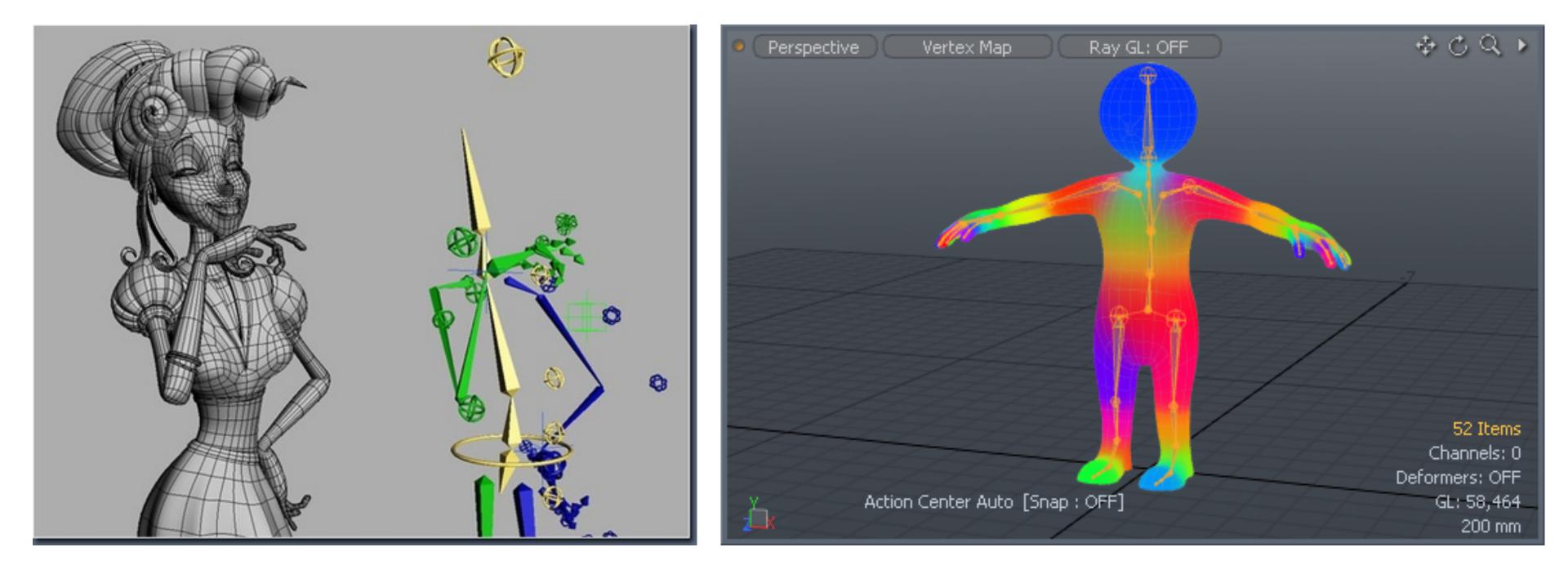
- Important technique in animation and robotics
- Rather than adjust individual transformations, set "goal" and use algorithm to come up with plausible motion:



Many algorithms—to be discussed in a future lecture

Skeletal animation

- Previous characters looked a lot different from "cube man"!
- Often use "skeleton" to drive deformation of continuous surface
- Influence of each bone determined by, e.g., weighting function:

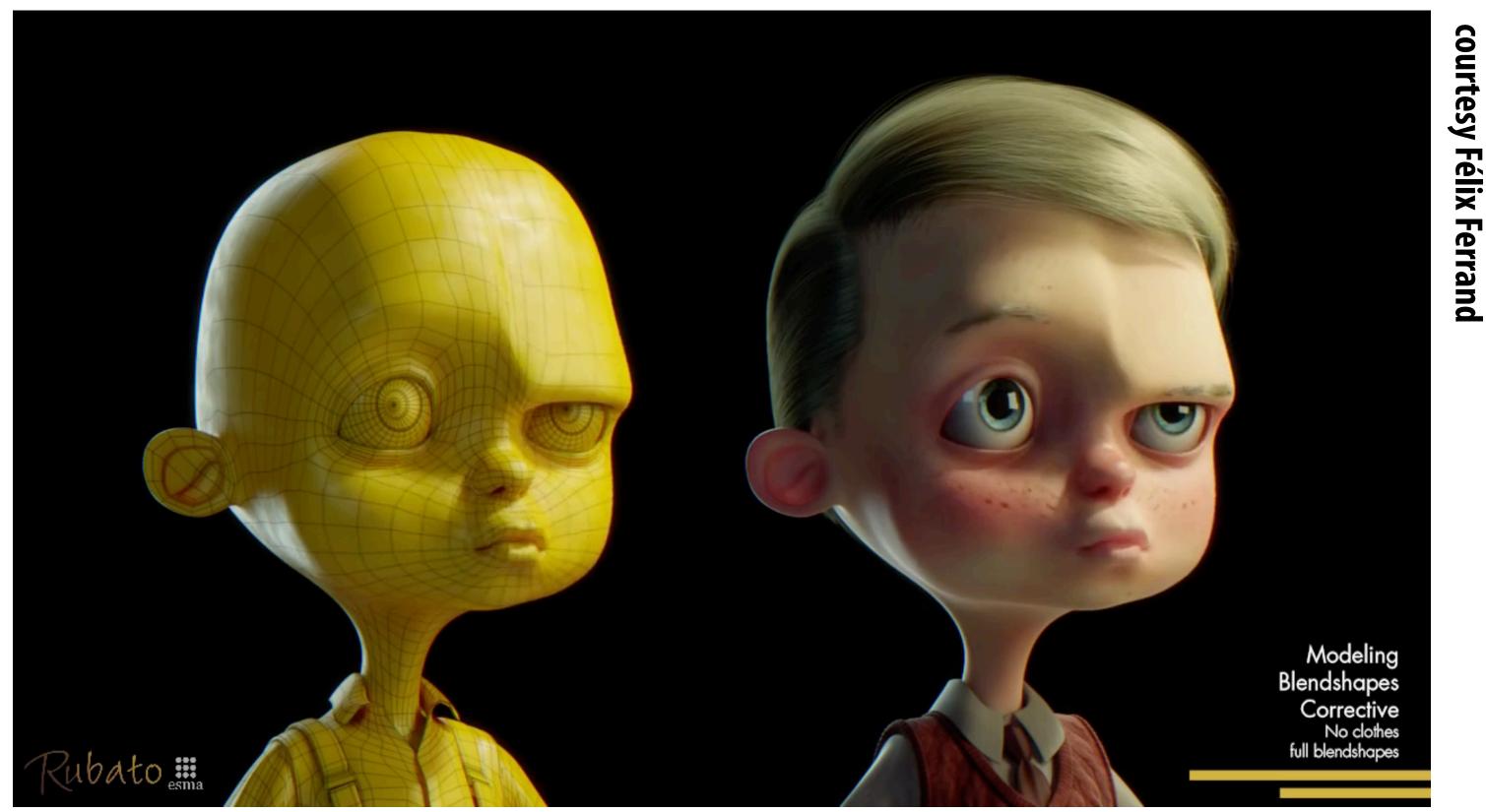


(Many, many other possibilities—still active area of R&D)

nt from "cube man"! on of continuous surface e.g., weighting function:

Blend shapes

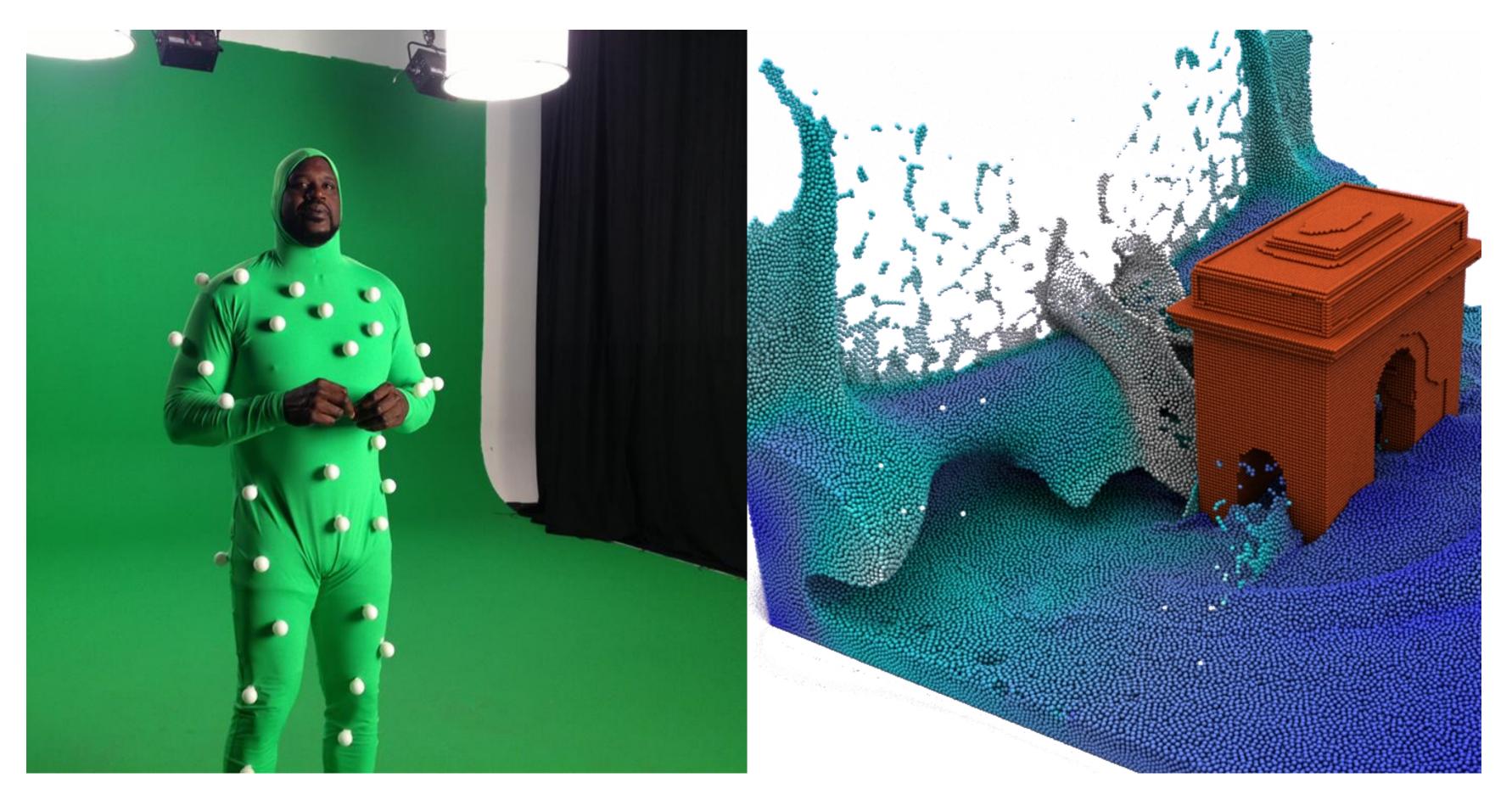
- Instead of skeleton, interpolate directly between surfaces
- E.g., model a collection of facial expressions:



Simplest scheme: take linear combination of vertex positions Spline used to control choice of weights over time

Coming up next...

- Even with "computer-aided tweening," animating a scene by hand takes a lot of work!
- Will see how data capture and physical simulation can help



Principles of animation

Animation principles

From

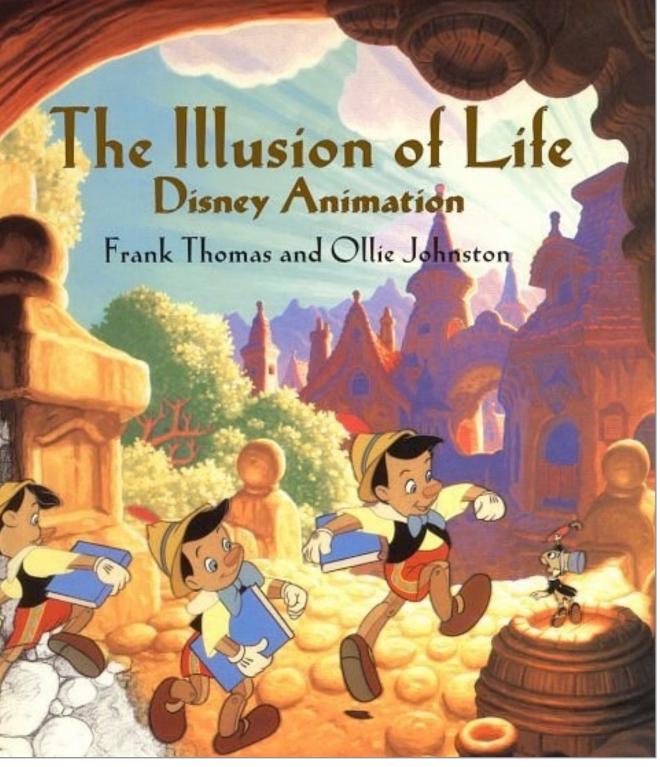
 "Principles of Traditional Animation Applied to 3D **Computer Animation**" - John Lasseter, ACM Computer Graphics, 21(4), 1987

In turn from

- "The Illusion of Life" **Frank Thomas and Ollie Johnson**



http://www.siggraph.org/education/materials/HyperGraph/animation/character animation/principles/prin trad anim.htm



12 animation principles

- 1. Squash and stretch
- 2. Anticipation
- 3. Staging
- 4. Straight ahead and pose-to-pose
- 5. Follow through
- 6. Ease-in and ease-out
- **7.** Arcs
- 8. Secondary action
- 9. Timing
- 10. Exaggeration
- 11. Solid drawings
- 12. Appeal

12 animation principles

THE ILLUSION OF LIFE

Cento Lodgiani, <u>https://vimeo.com/93206523</u>





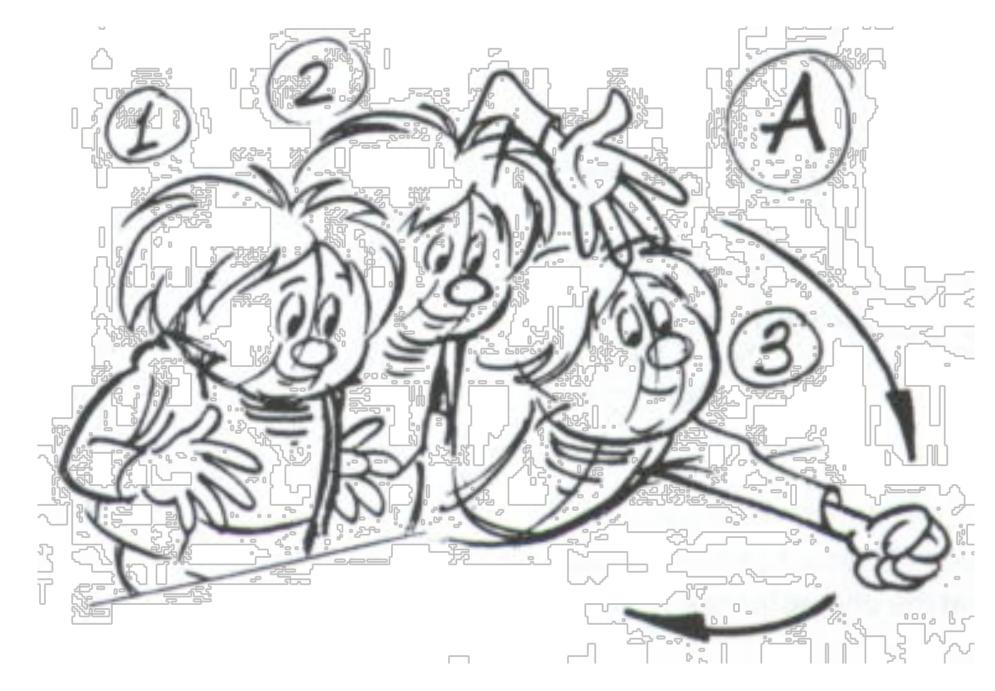
Squash and stretch

- Refers to defining the rigidity and mass of an object by distorting its shape during an action
- Shape of object changes during movement, but not its volume



Anticipation

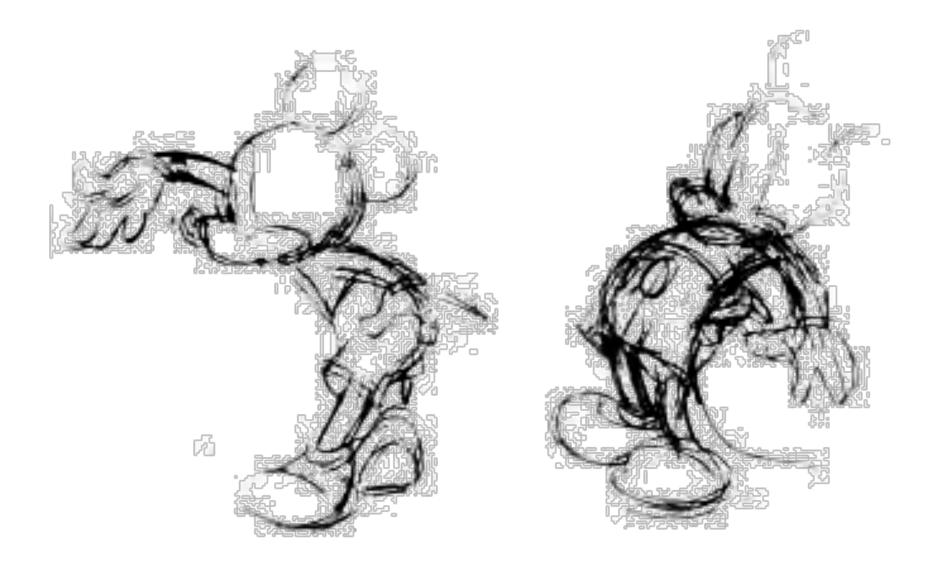
- **Prepare for each movement**
- For physical realism
- To direct audience's attention



Timing for Animation, Whitaker & Halas

Staging

- Picture is 2D
- Make situation clear
- Audience looking in right place
- Action clear in silhouette



Disney Animation: The Illusion of Life



Follow through

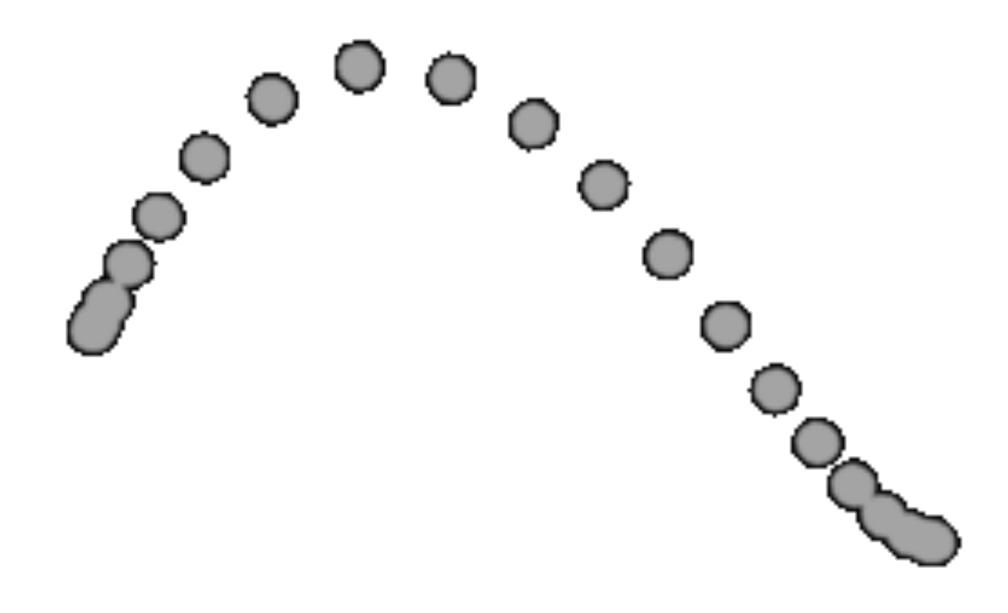
- **Overlapping motion**
- Motion doesn't stop suddenly
- **Pieces continue at different rates**
- **One motion starts while previous is** finishing, keeps animation smooth



Timing for Animation, Whitaker & Halas

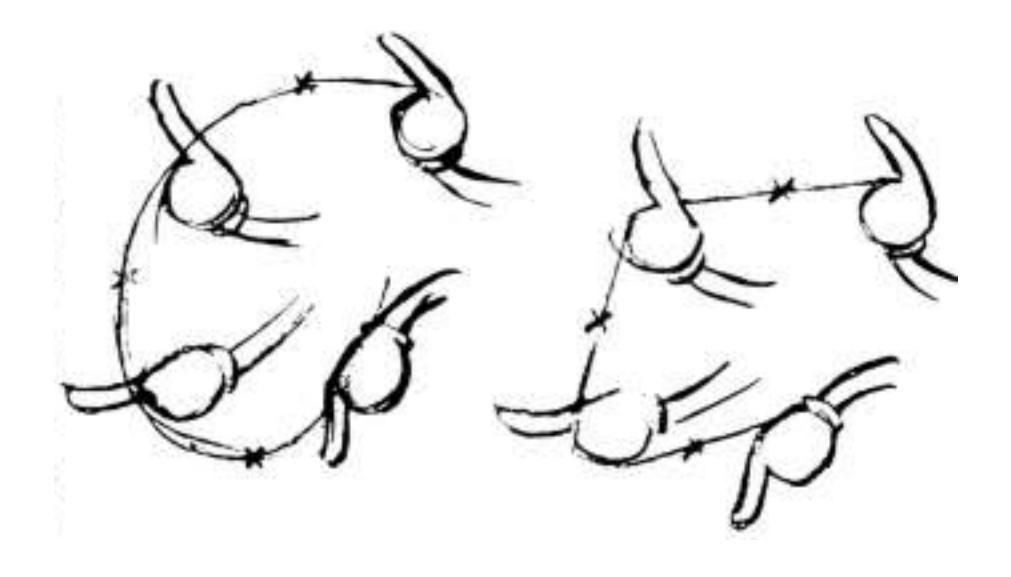
Ease-in and ease-out

Movement doesn't start and stop abruptly Also contributes to weight and emotion



Arcs

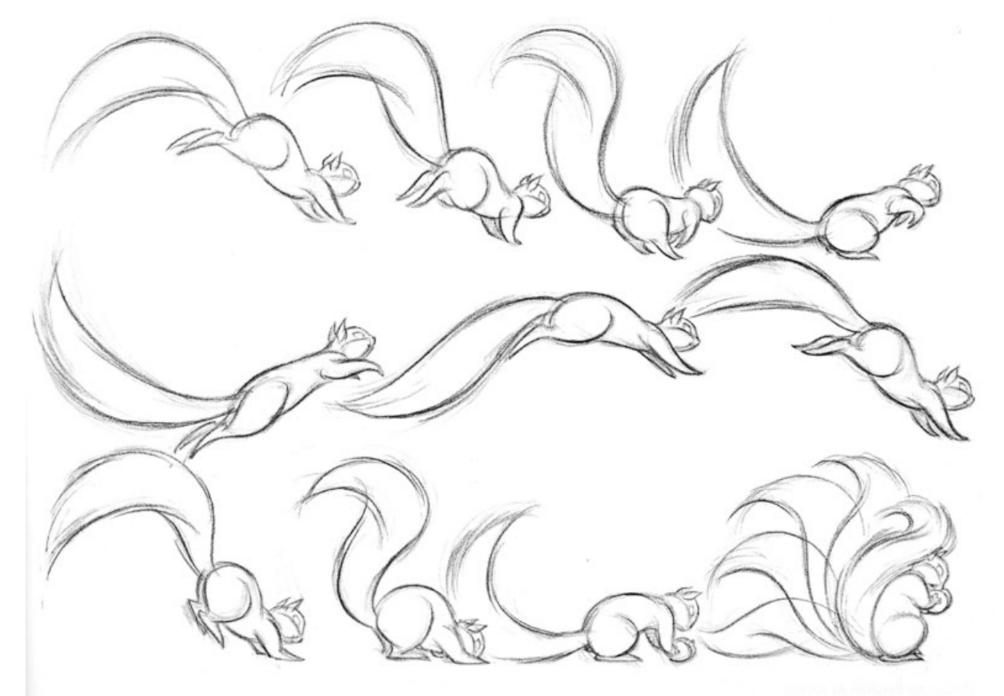
Move in curves, not in straight lines This is how living creatures move



Disney Animation: The Illusion of Life

Secondary action

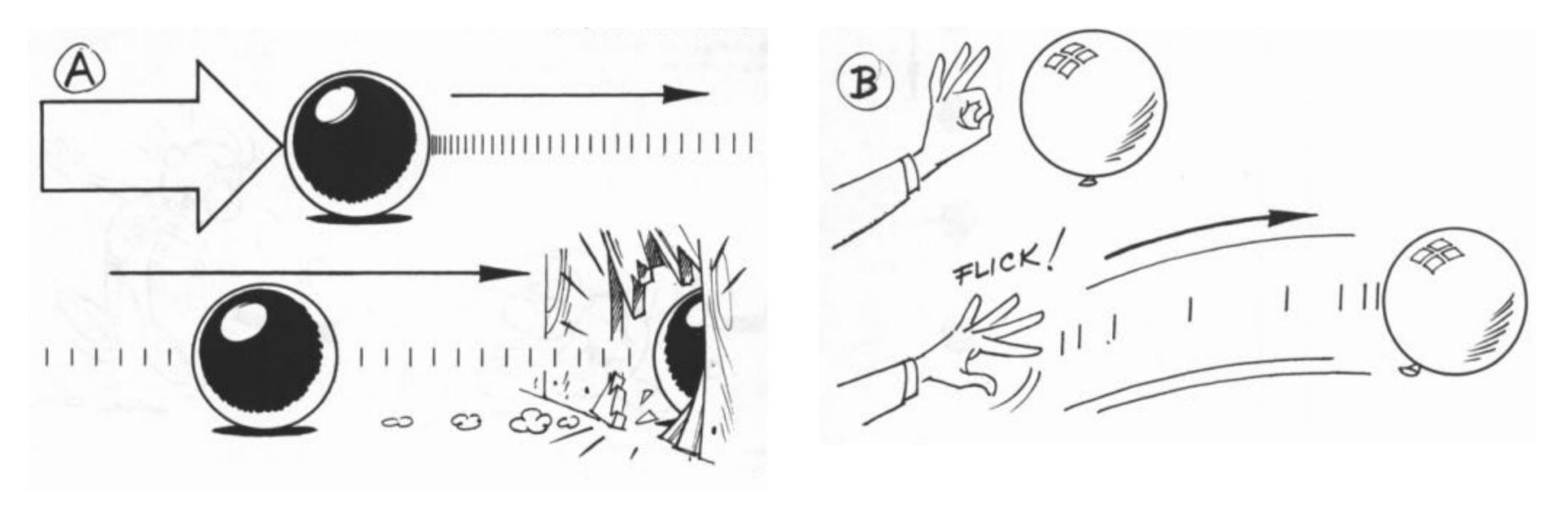
- Motion that results from some other action
- **Needed for interest and realism**
- Shouldn't distract from primary motion



Cartoon Animation, Preston Blair

Timing

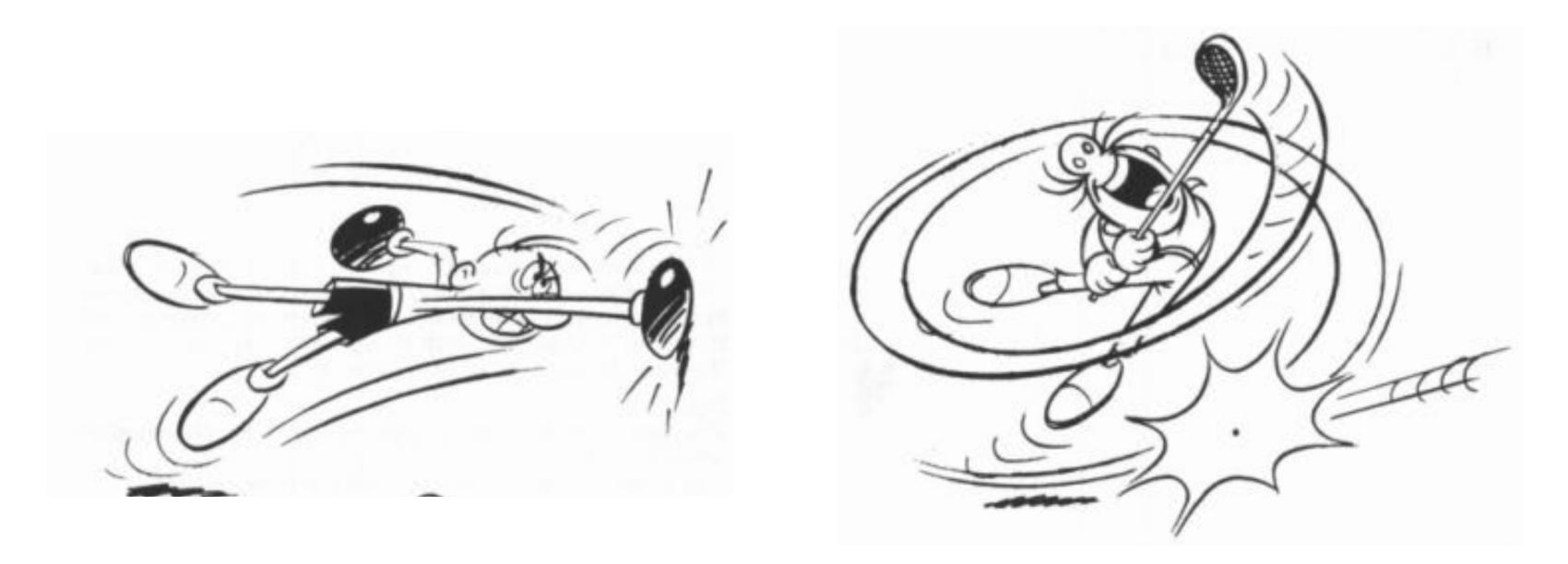
- Rate of acceleration conveys weight
- Speed and acceleration of character's movements convey emotion



Timing for Animation, Whitaker & Halas

Exaggeration

- Helps make actions clear
- Helps emphasize story points and emotion
- Must balance with non-exaggerated parts



Timing for Animation, Whitaker & Halas

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Appeal

Attractive to the eye, strong design

Avoid symmetries



Disney Animation: The Illusion of Life

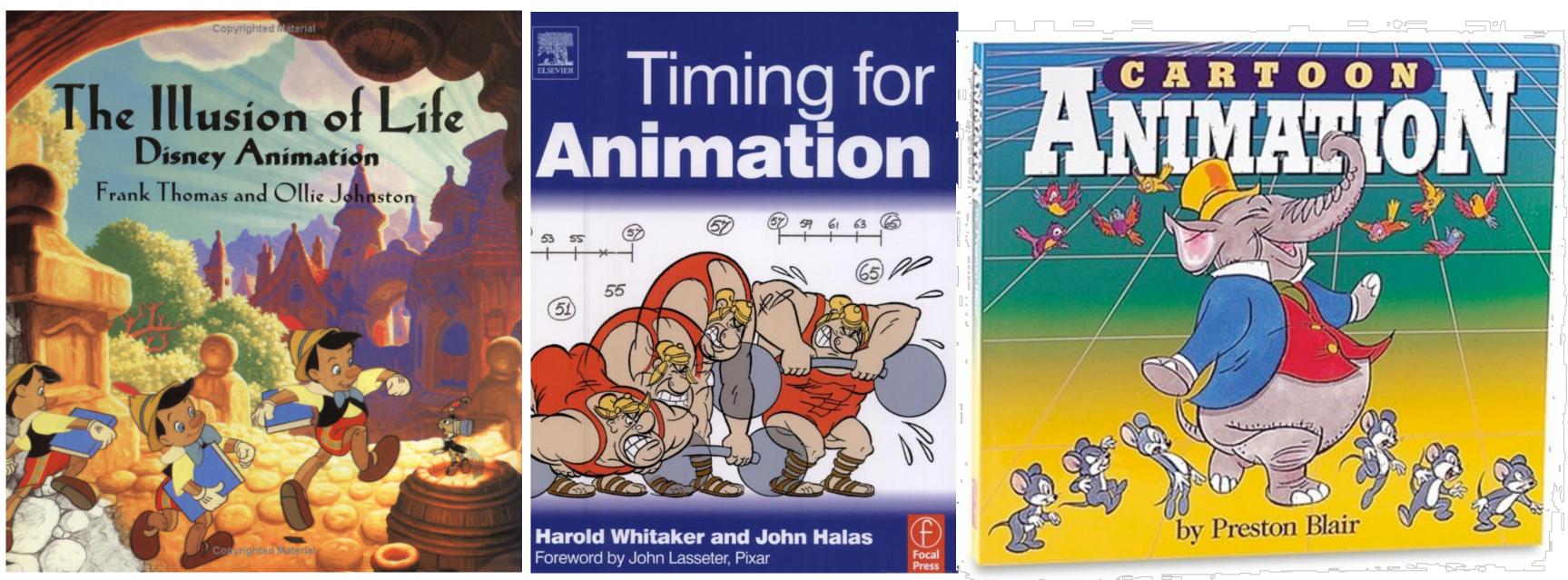
Personality

- Action of character is result of its thoughts
- Know purpose and mood before animating each action
- No two characters move the same way



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Further reading



Acknowledgements

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